

0. NOTATION

0.0.1 The Greek Alphabet

A, α	alpha	H, η	eta	N, ν	nu	T, τ	tau
B, β	beta	Θ, θ	theta	Ξ, ξ	xi	Y, υ	upsilon
Γ, γ	gamma	I, ι	iota	O, \omicron	omicron	Φ, ϕ, φ	phi
Δ, δ	delta	K, κ	kappa	Π, π	pi	X, χ	chi
E, ϵ	epsilon	Λ, λ	lambda	P, ρ, ϱ	rho	Ψ, ψ	psi
Z, ζ	zeta	M, μ	mu	$\Sigma, \sigma, \varsigma$	sigma	Ω, ω	omega

0.0.2 Set Theory and Functions

\mathbb{R}	the set of real numbers;
\mathbb{C}	the set of complex numbers;
\mathbb{Q}	the set of rational numbers — i.e. the fractions,
\mathbb{Z}	the set of integers — i.e. the whole numbers;
\mathbb{N}	the set of natural numbers — i.e. the non-negative whole numbers;
\mathbb{R}^n	n -dimensional real space — i.e. the set of all real n -tuples (x_1, x_2, \dots, x_n) ;
$\mathbb{R}[x]$	the set of polynomials in x with real coefficients;
\in	is an element of — e.g. $\sqrt{2} \in \mathbb{R}$ and $\pi \notin \mathbb{Q}$;
\subseteq, \subset	is a subset of — e.g. $\mathbb{N} \subseteq \mathbb{Z} \subseteq \mathbb{Q} \subseteq \mathbb{R} \subseteq \mathbb{C}$;
$ X $	the <i>cardinality</i> (size) of the set X ;
$X \cup Y$	the <i>union</i> of two sets — read ‘cup’ — $\{s : s \in X \text{ or } s \in Y\}$;
$X \cap Y$	the <i>intersection</i> of two sets — read ‘cap’ — $\{s : s \in X \text{ and } s \in Y\}$;
$X \times Y$	the <i>Cartesian product</i> of X and Y — $\{(x, y) : x \in X \text{ and } y \in Y\}$;
$X - Y$ or $X \setminus Y$	the <i>complement</i> of Y in X — $\{s : s \in X \text{ and } s \notin Y\}$;
\emptyset	the empty set.
$f : X \rightarrow Y$	f is a function, map, mapping from a set X to a set Y ; X is called the <i>domain</i> and Y is called the <i>codomain</i> ;
$f(X)$ or $f[X]$	the <i>image</i> or <i>range</i> of the function f — i.e. the set $\{f(x) : x \in X\}$;
$g \circ f$	the <i>composition</i> of the maps g and f — do f first then g ;
f is <i>injective</i> or <i>1-1</i>	if $f(x) = f(y)$ then $x = y$;
f is <i>surjective</i> or <i>onto</i>	for each $y \in Y$ there exists $x \in X$ such that $f(x) = y$;
f is <i>bijective</i>	f is <i>1-1</i> and <i>onto</i> ;
f is <i>invertible</i>	there exists a function $f^{-1} : Y \rightarrow X$ s.t. $f \circ f^{-1} = id_Y$ and $f^{-1} \circ f = id_X$;