

Quantifiers: for all

Quantifiers: for all

Given a statement with a variable, we can make it into an unconditional statement with “for all”:

Quantifiers: for all

Given a statement with a variable, we can make it into an unconditional statement with “for all”:

- ▶ n is prime.

depends on the variable n .

Quantifiers: for all

Given a statement with a variable, we can make it into an unconditional statement with “for all”:

- ▶ n is prime.

depends on the variable n . But

Quantifiers: for all

Given a statement with a variable, we can make it into an unconditional statement with “for all”:

- ▶ n is prime.

depends on the variable n . But

- ▶ n is prime for all integers n

does not depend on the value of a variable.

Quantifiers: for all

Given a statement with a variable, we can make it into an unconditional statement with “for all”:

- ▶ n is prime.

depends on the variable n . But

- ▶ n is prime for all integers n

does not depend on the value of a variable.

Lots of variations in wording:

Quantifiers: for all

Given a statement with a variable, we can make it into an unconditional statement with “for all”:

- ▶ n is prime.

depends on the variable n . But

- ▶ n is prime for all integers n

does not depend on the value of a variable.

Lots of variations in wording:

- ▶ For every integer n , n is prime.
- ▶ Every integer is prime.
- ▶ If n is an integer, then n is prime.
- ▶ Let n be an integer. Then n is prime.

Quantifiers: there exists

Quantifiers: there exists

We can also use “there exists” to make a variable statement into an unconditional statement:

Quantifiers: there exists

We can also use “there exists” to make a variable statement into an unconditional statement:

- ▶ There exists an integer n such that n is prime does not depend on the value of a variable.

Quantifiers: there exists

We can also use “there exists” to make a variable statement into an unconditional statement:

- ▶ There exists an integer n such that n is prime does not depend on the value of a variable.

Variations in wording:

Quantifiers: there exists

We can also use “there exists” to make a variable statement into an unconditional statement:

- ▶ There exists an integer n such that n is prime does not depend on the value of a variable.

Variations in wording:

- ▶ n is prime for some integer n .
- ▶ There is a prime integer.

More examples

More examples

- (a) There is a student who hasn't done the week 1 quiz. (true)

More examples

- (a) There is a student who hasn't done the week 1 quiz. (true)
- (b) Every student will do the week 2 quiz. (true)

More examples

- (a) There is a student who hasn't done the week 1 quiz. (true)

- (b) Every student will do the week 2 quiz. (true)

- (c) $x + 1 > x$ for all real numbers x . (true)

More examples

- (a) There is a student who hasn't done the week 1 quiz. (true)
- (b) Every student will do the week 2 quiz. (true)
- (c) $x + 1 > x$ for all real numbers x . (true)
- (d) $n^2 > 10$ for every integer n . (false)

More examples

- (a) There is a student who hasn't done the week 1 quiz. (true)

- (b) Every student will do the week 2 quiz. (true)

- (c) $x + 1 > x$ for all real numbers x . (true)

- (d) $n^2 > 10$ for every integer n . (false)

- (e) There is an integer n such that $n^2 > 10$. (true)

More examples

- (a) There is a student who hasn't done the week 1 quiz. (true)

- (b) Every student will do the week 2 quiz. (true)

- (c) $x + 1 > x$ for all real numbers x . (true)

- (d) $n^2 > 10$ for every integer n . (false)

- (e) There is an integer n such that $n^2 > 1000$.

More examples

- (a) There is a student who hasn't done the week 1 quiz. (true)

- (b) Every student will do the week 2 quiz. (true)

- (c) $x + 1 > x$ for all real numbers x . (true)

- (d) $n^2 > 10$ for every integer n . (false)

- (e) There is an integer n such that $n^2 > 1000$. (true)

More examples

- (a) There is a student who hasn't done the week 1 quiz. (true)

- (b) Every student will do the week 2 quiz. (true)

- (c) $x + 1 > x$ for all real numbers x . (true)

- (d) $n^2 > 10$ for every integer n . (false)

- (e) There is an integer n such that $n^2 > 1000000$.

More examples

- (a) There is a student who hasn't done the week 1 quiz. (true)
- (b) Every student will do the week 2 quiz. (true)
- (c) $x + 1 > x$ for all real numbers x . (true)
- (d) $n^2 > 10$ for every integer n . (false)
- (e) There is an integer n such that $n^2 > 1000000$. (true)