### MTH5123 Differential Equations Introductory slides

Prof. Ginestra Bianconi School of Mathematical Sciences, Queen Mary University of London



#### What are ordinary differential equations?

An ordinary differential equation of order n for a function y(t)

is an equation of the form

$$\mathscr{F}\left(\frac{d^n y}{dt^n}, \frac{d^{n-1} y}{dt^{n-1}}, \dots, \frac{dy}{dt}, y, t\right) = 0$$

(where the 
$$n-th$$
 derivative  $\displaystyle rac{d^n y}{dt^n}$  occurs in  $\mathscr{F}$ )

The variable *t* is called the independent variable,

the variable y is called the dependent variable

#### Isaac Newton (25 December 1642 – 20 March 1726)

Driven by the need to understand

the physical word

including gravitation and mechanics

Isaac Newton founded Calculus



#### Classical mechanics: the birth of differential equations

At time t=0 you launch a mass vertically from a given height h at a given velocity  $v_0$ .

- Which is the height of the mass at time t?
- When does this mass reach the floor?
- At which velocity does it reach the floor?

$$m\ddot{y} = -mg$$

$$y(0) = h$$
$$\dot{y}(0) = v_0$$

# Modelling epidemic spreading

#### You want to model a pandemic

- What is the dynamics for a given  $R_0$ ?
- How many would be the removed individuals (immunised or deceased) at time *t*?
- The SIR dynamics involving a given fraction of susceptible *S*, infected *I* and removed individuals *R*

$$S + I + R = 1$$

$$\dot{I} = R_0 I (1 - I - R) - I$$
$$\dot{R} = I$$

$$I(0) = I_0$$
$$R(0) = R_0$$

#### Financial mathematics: Continuously Varying Interest Rates

Suppose you put *x* in your bank account at time t = 0, and the interest is continuously compounded with a rate r(t) that changes in times.

• What is the amount *D*(*t*) that you will have in your account at time *t*?

$$\dot{D}(t) = D(t)r(t) \qquad \qquad D(0) = x$$

#### MTH5123: Applied mathematics module

The module intends to build on your First and Second Year mathematical knowledge of

> Calculus Algebra

to give you the skills of being able to solve

**Ordinary Differential equations** 

to address questions emerging in a variety of applications

Including physics, biology, finance etc.



Therefore it is important that you refresh your Calculus

In the Welcome Week please prepare

#### for the Differential Equations module

by

answering the

**Revision questions of pre-request knowledge from previous modules** 

posted in the QM+ page under Week 1

# **Lectures and Tutorials**

- Schedule:
- Lesson 1-2 Tuesday 11:00-13:00 Live Arts Two LT
- Lesson 3 Tuesday 14:00-15:00 Live Arts Two LT

You will be assigned to one of the following three tutorials (check your timetable to know which applies)

- Tutorial 1: Thursday 12:00-13:00 PP2
- Tutorial 2: Thursday 16:00-17:00 Bancroft 1.13
- Tutorial 3: Thursday 17:00-18:00 Graduate Ctr:GC201

### **Lectures and Tutorials**

#### Your tasks:

- Make an effort to attend the lecture live
- Take your own notes while attending the lecture
- Ask questions
- Complete formative assements, and mock quizzes and submit courseworks

### Lecture notes

- Lecture note material available on QMPlus:
- Typed in lecture notes
- Handwritten lecture notes
- Your tasks:
- Read the typed in lecture notes in advance of the lectures
- Study the notes after the lecture to check your full understanding of the module material.

# **Reading list**

- J. C. Robinson: An introduction to Ordinary Differential Equations (Cambridge University Press)
- Available from the library! (See link in QM+)

# **Good practice**

Train yourself in deriving the solution

of differential equations with pen and pencil!!

This is of fundamental importance for the preparation to the final exam

A good mathematicians is like a good athlete:

he or she needs a lot of training and commitment!!

To check your solutions you can also help your study with numerical software such as Mathematica of MATLAB

See QM+ for an example of a Mathematica notebook

and link to QM student licence

### **Formative Assessment**

- Each week, at the tutorial we will cover
- The formative assignment and the mock quiz for the week, available on the QMPlus page
- Your task:
- Attempt the formative assessment and the mock quiz before the tutorial
- Ask questions regarding the coursework during the tutorial

#### Assessed courseworks

- Every assessed coursework is worth 10% of the final marks
- You will have one week to complete assessed courseworks
- The 2 assessed courseworks will be posted in weeks 6,11

### Final exam

• The final exam will account for 80% of the final mark

#### Feedback

Feedback on your assessed coursework:

**Personalised feedback** 

Quiz questions: You will be able to see your scores soon after the submission deadline

#### **General feedback**

General feedback will be given during the online tutorial

where we will go over the most challenging questions of the assessed

courseworks and the common mistakes.

# **Online Forum**

For any question on the module material that you would like to ask there are two ways to received feedback and answers:

- You can ask the question during the live lectures and tutorials
- You can post the question on the online forum

Participation to the online forum is highly beneficial as it increases the interactions between fellow students.

The online forum will be monitored twice a week

#### Welcome to the Differential Equations module!

See you at the first lecture

#### 11:00-13:00, Tuesday 27 September 2022