



Queen Mary
University of London



Mass Transfer and Separations Processes I

Revision Lecture

DEN5406

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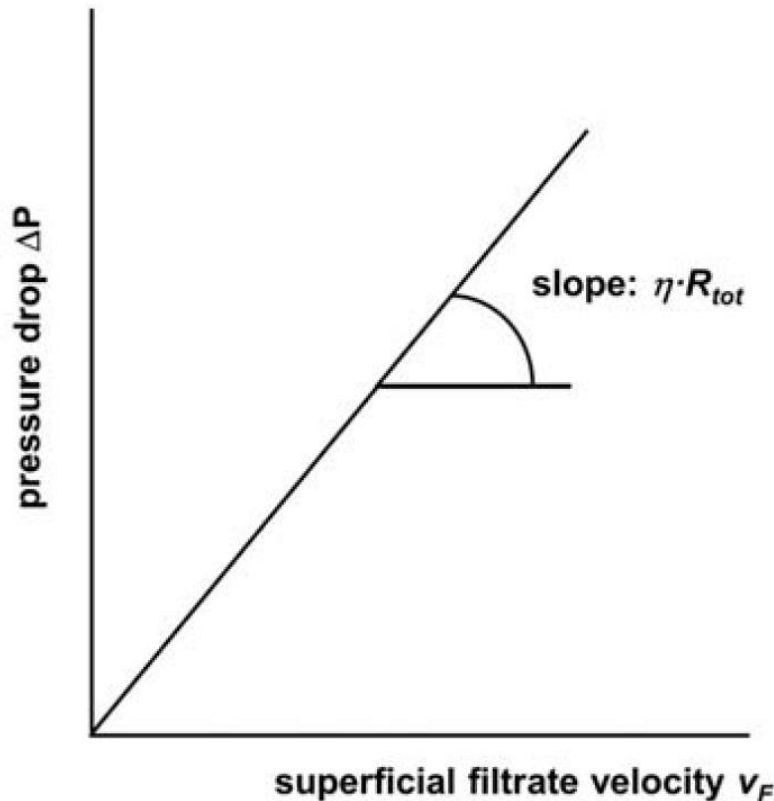
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www.aimlabs.org

Outline

1. Cooking – intro – learn concepts – but also solve them in Excel
2. Purifying dirty water – to drink
 - a. Sterilizing methods – kill or remove pathogens - membrane
 - b. Purifying from chemicals – distillation – in space
 - c. Freezing for purification
 - d. Separating Azeotropes
 - e. Desalination by ion exchange and reverse osmosis
3. Purifying dirty oil - > so it can be used as fuel, or not spoil
 - a. Mechanical separation – filtration
 - b. Mechanical separation – centrifugation
4. Extraction from Solids
 - a. Espresso from ground beans
 - b. Extracting oil from pressed beans and olives
 - c. Leaching metals from ores
5. Drying solids – preserving foods
 - a. Getting rid of water or stripping the water

Filtration – Quantitation



$$v_F = \frac{\Delta P}{\eta (R_M + R_C)}$$

Resistance due to filter medium
And to cake (R_M and R_C)

$$v_F = \frac{1}{A} \frac{dV}{dt}$$

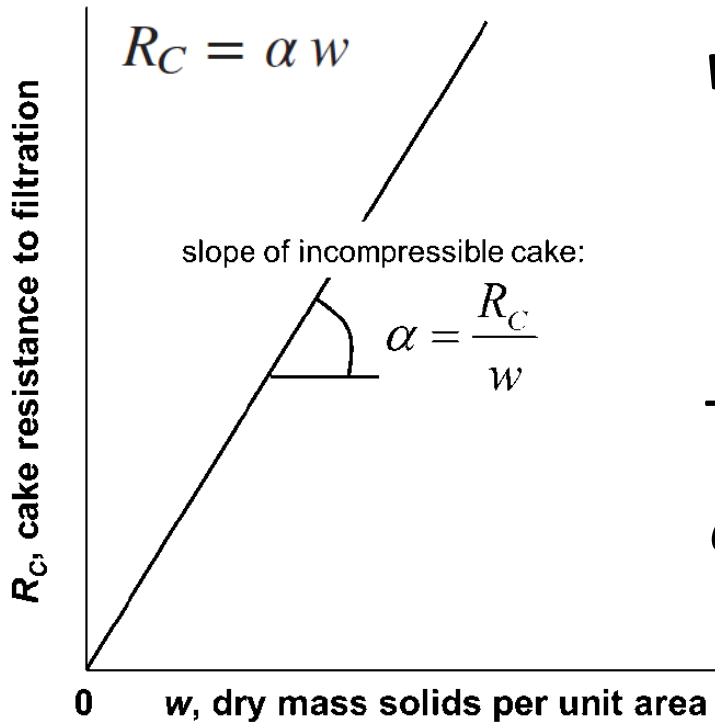
$$\Delta P = \Delta P_C + \Delta P_M = \eta \frac{R_C + R_M}{A} \frac{dV}{dt}$$

Darcy's Law

Filtration – Incompressible Cake

Incompressible cake causes:

a *linear* increase in resistance R_C with *cake height*



w is mass dry solids per filter area A
 $w = \frac{c V}{A}$ [kg/m²] where c is kg solids
 per volume V of suspension

The proportionality slope R_C / w is
 α - the specific cake resistance [m/kg]

Darcy's Law with specific resistance:

$$\eta \frac{R_C + R_M}{A} \frac{dV}{dt} \Rightarrow$$

$$\Delta P = \frac{\eta c \alpha}{A^2} V \frac{dV}{dt} + \frac{\eta R_M}{A} \frac{dV}{dt}$$

Simple

vs.

Flash Distillation

Same, yet

Batch

vs.

Continuous

$$y = \frac{\alpha x}{1 + (\alpha - 1)x} \quad \text{with} \quad \alpha = \frac{K_A}{K_B}$$

Single stage separation efficiency.

Relative volatility α is the equilibr.

VL- constant, also referred to as K

continuous feed is partially vaporized to give a vapor richer in the more volatile components.

limited degree of separation

Uses: e.g. seawater desalination,

Where bp differences are high

Above is derived from Two Mass Balances –
One for whole liquid, one for a component in the liquid

$$F = V + L \quad \text{and} \quad Fz = Vy + Lx$$

Here F is the total fluid and
 V, L – vapor and liquid separated

z, y, x , and the mole fractions of
a component in fluid, vapor, liquid

Multi-Stage and Column Distillation

with Rectification

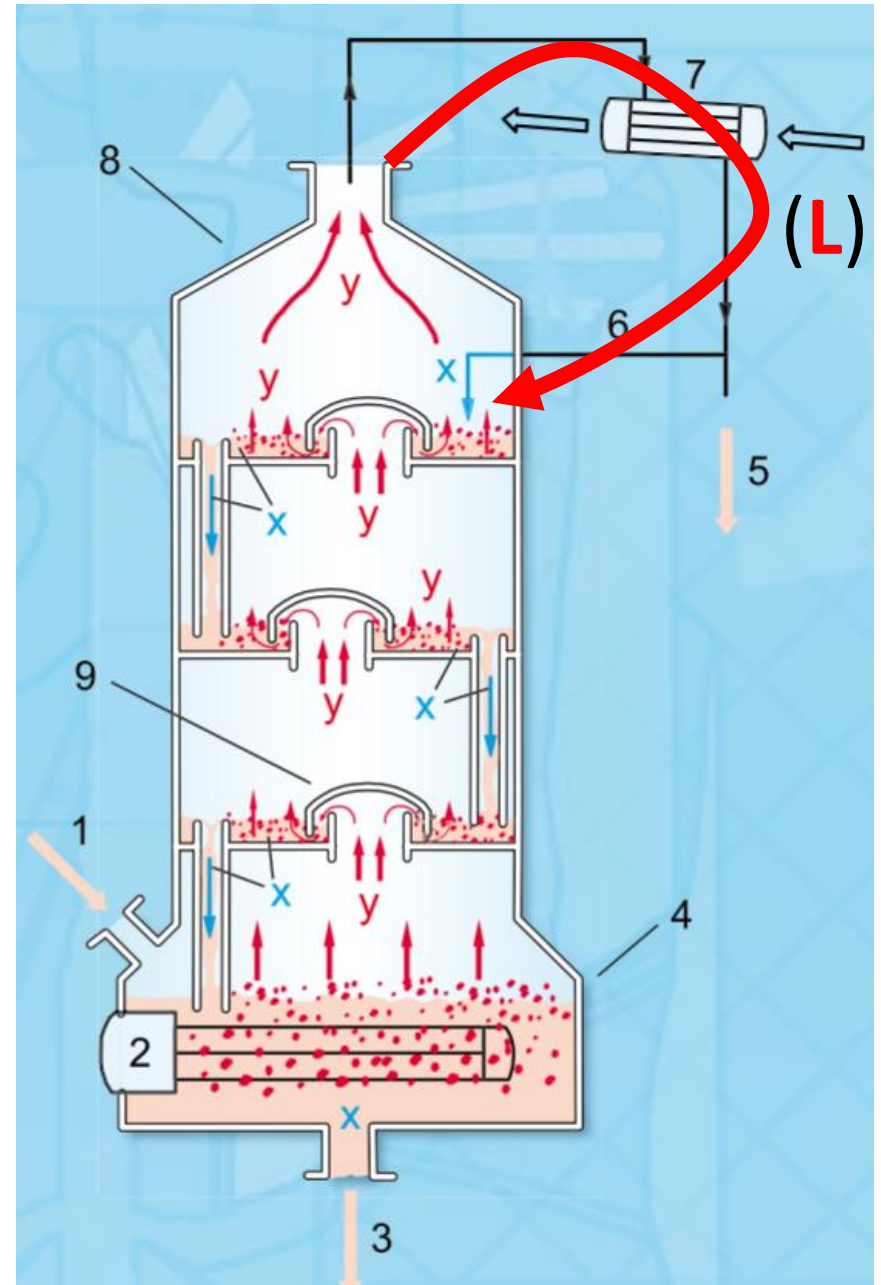
Top vapor = product

Part condensed, fed back

Words for vocabulary:

distillation column, Reflux,
rectification, reflux ratio,
reboiler, Operating pressure

The **Reflux ratio** $R = L/D$ is
the ratio of reflux flow (**L**)
to distillate flow (**D**)
(**L** Being returned back to the
column for re-distilling)



Two-Phase Equilibria

In Distillation

$$K_i \equiv \frac{y_i}{x_i}$$

distribution coefficient K_i
between phases x,y of
component i

$$\alpha_{ij} = \frac{K_i}{K_j} :$$

the **relative volatility** of *i*
Determines the selectivity of
Separation vs a reference *j* is

How do we measure relative volatility?

$$p_i = y_i P_{tot}$$

Dalton's law relates concentration of
components in an ideal gas or to
partial pressures in the vapor mixture

$$p_i = x_i P_i^0$$

Raoult's law gives partial pressure
in the vapor (p_i) from concentr.
in the liquid (x_i) mixture

Combination gives:

$$y_i P_{tot} = x_i P_i^0 \quad K_i = \frac{y_i}{x_i} = \frac{P_i^0}{P_{tot}} \quad \text{and}$$

$$\alpha_{ij} = \frac{K_i}{K_j} = \frac{P_i^0}{P_j^0}$$

Operating condition: T and L/V

Graphical Determination – Mole Fractions

When we specify T, we can also

Decide on q

$$q = \frac{L}{F} = \frac{\text{Fraction of feed remaining}}{\text{liquid}}$$

$$(1-q) = V / F \quad (\text{Fraction vaporized})$$

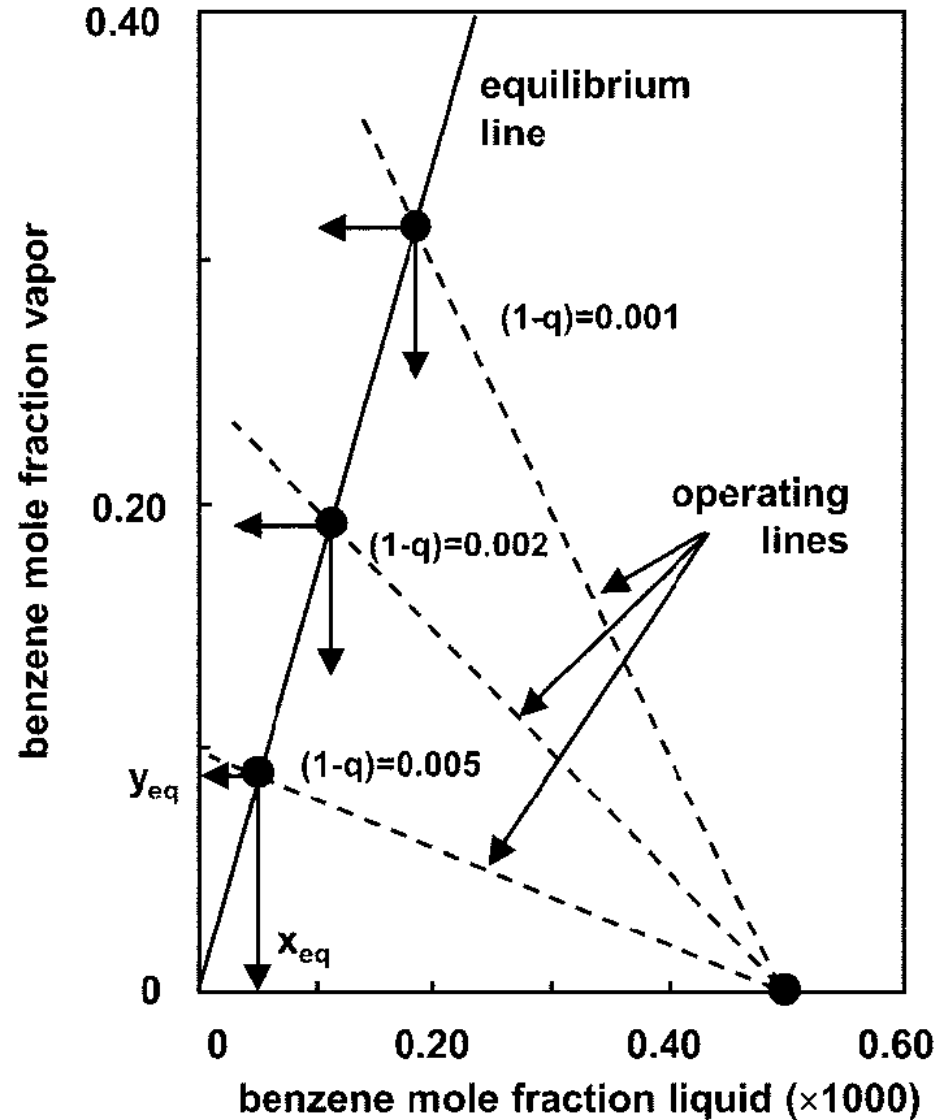
The **Operating Line** equation

is:

$$y = -\frac{q}{1-q} x + \frac{1}{1-q} z$$

The **Equilibrium line** is:

$$\frac{y}{1-y} = \alpha \cdot \frac{x}{1-x}$$



Operating condition: T and total Pressure P

Graphical Determination – Mole Fractions

Now we have to find q

$$q = \frac{L}{F} = \frac{\text{Fraction of feed remaining}}{\text{liquid}}$$

by eliminating x, y from the

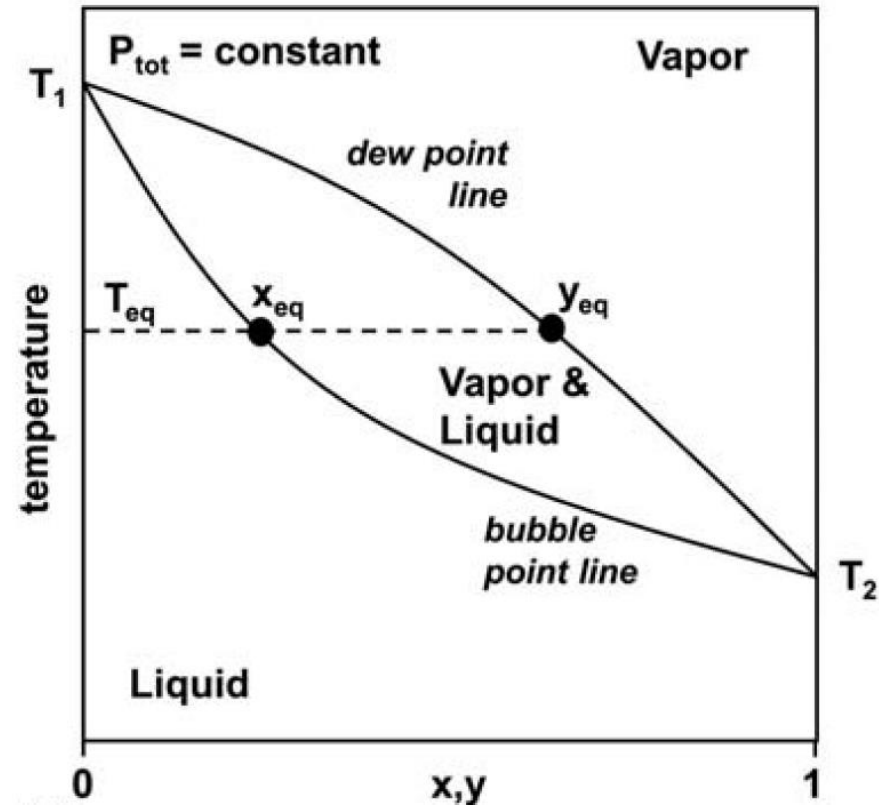
Operating Line equation:

$$y = -\frac{q}{1-q}x + \frac{1}{1-q}z$$

And **Equilibrium line:**

$$\frac{y}{1-y} = \alpha \cdot \frac{x}{1-x} \quad \text{given } T, P_{tot} - \text{the } K_i \text{ are known constants, so}$$

$$q = -z \frac{K_B}{1-K_B} - (1-z) \frac{K_A}{1-K_A} \quad \text{and} \quad x = \frac{1-K_B}{K_A-K_B}$$



McCabe-Thiele Analysis

Graphical Determination of # of equilibrium stages:

First:

Construct a staircase
Between
Operating lines and
Equilibrium curve.

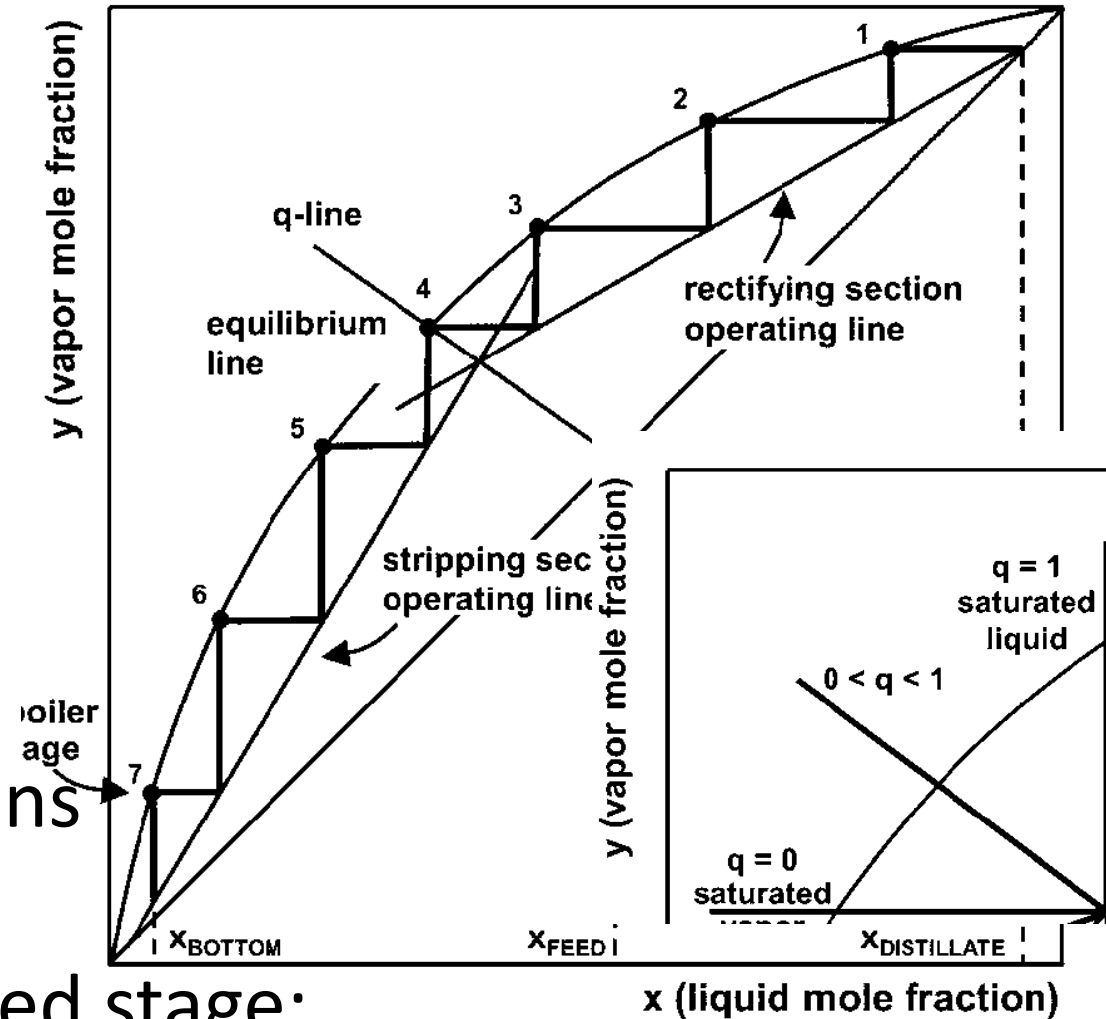
Horizontals – equil.

Verticals – compositions

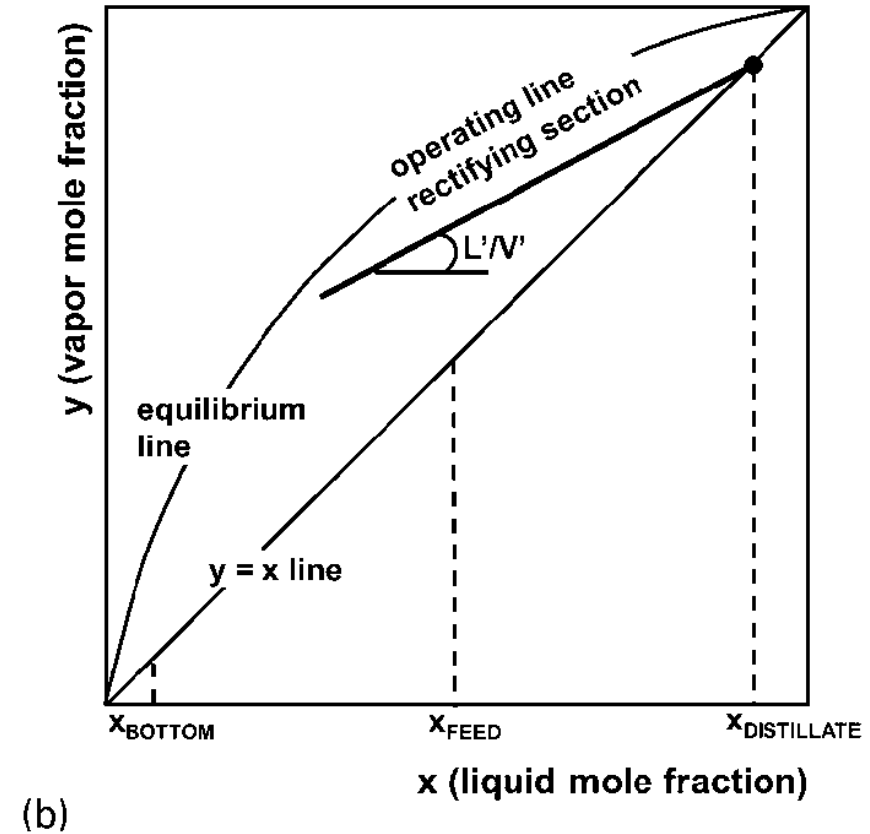
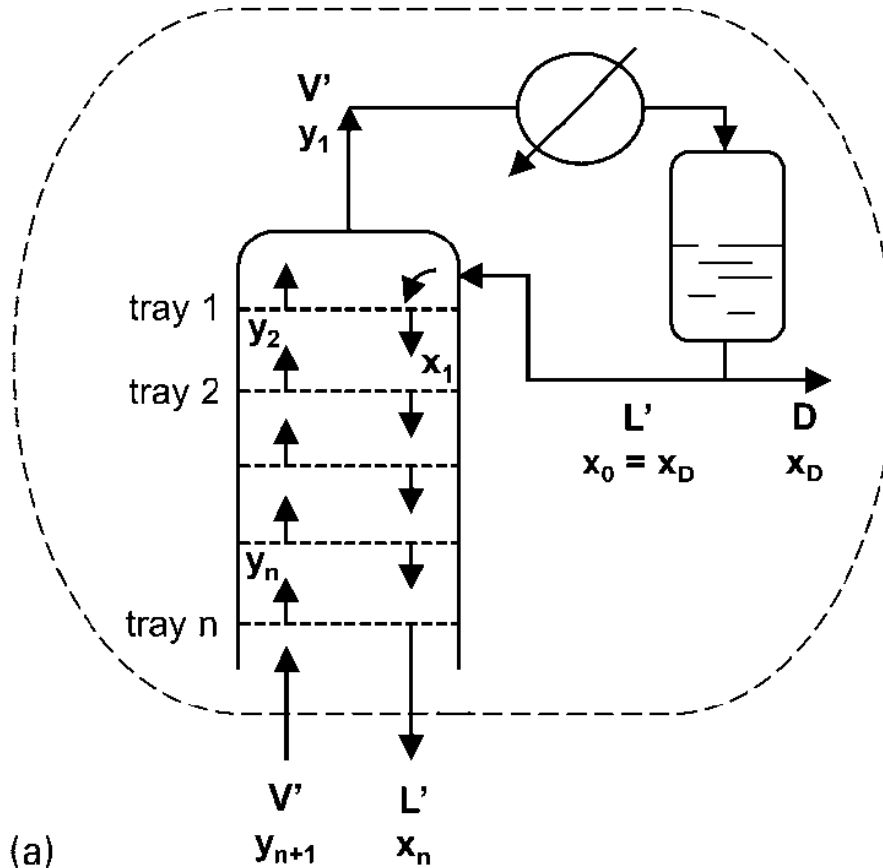
Passing each other

Optimal location of feed stage:

First location after horizontal crosses the q-line.



McCabe-Thiele Analysis

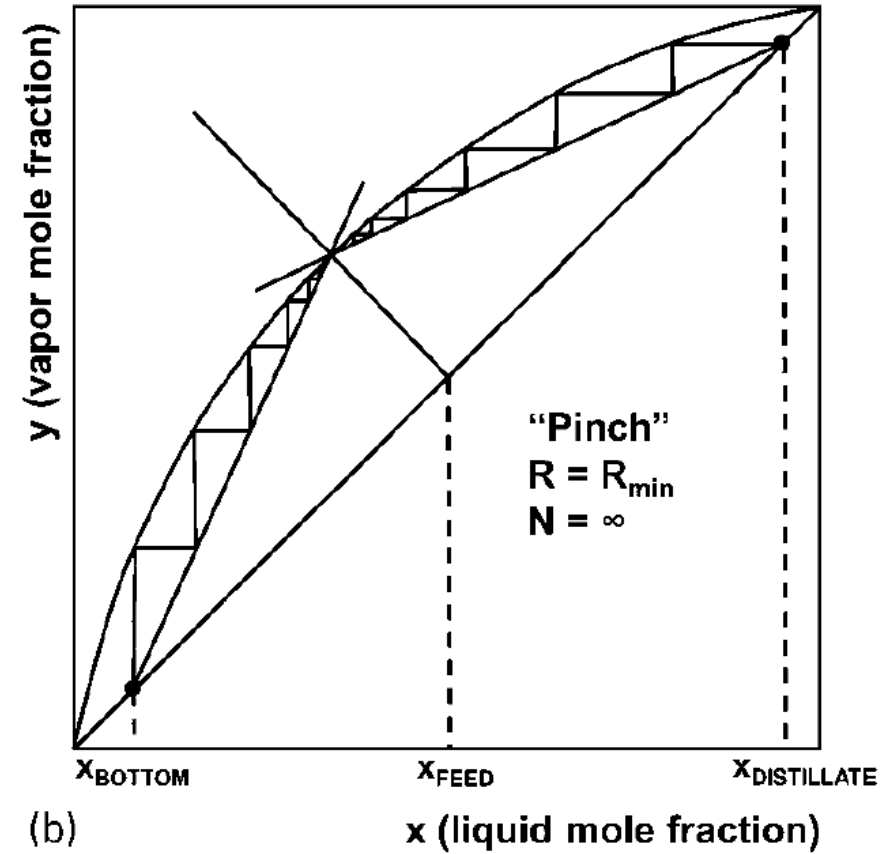
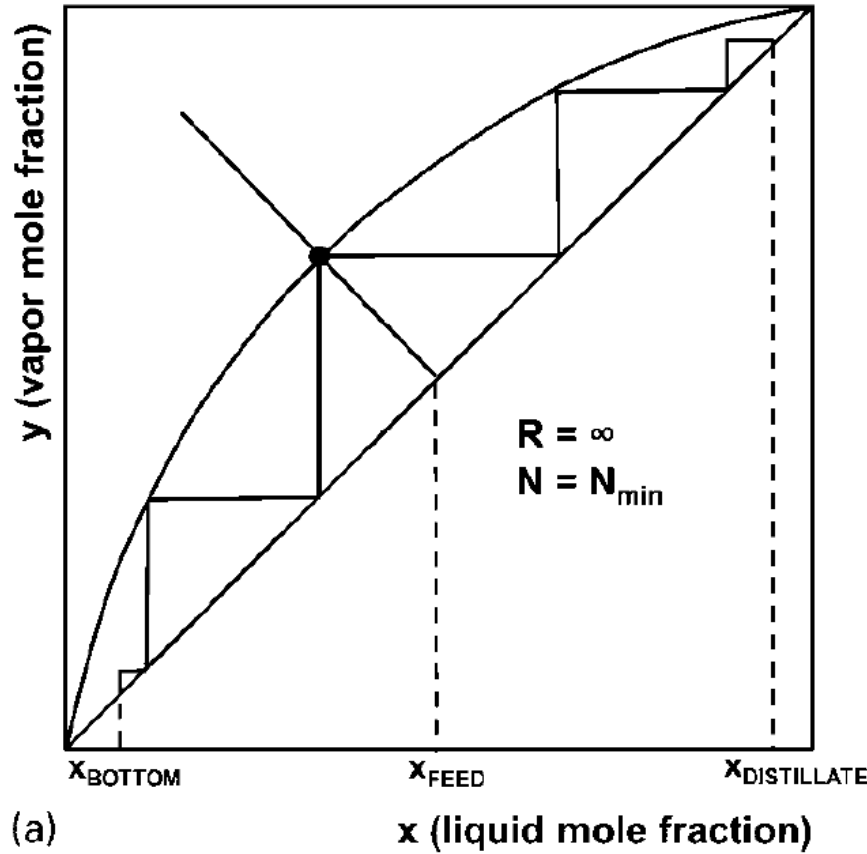


the **operating line** is a straight line in the y - x -diagram with an intersection at $y = x_D$ on the $y = x$ line, for **specified values of R and x_D** (purity of distillate)

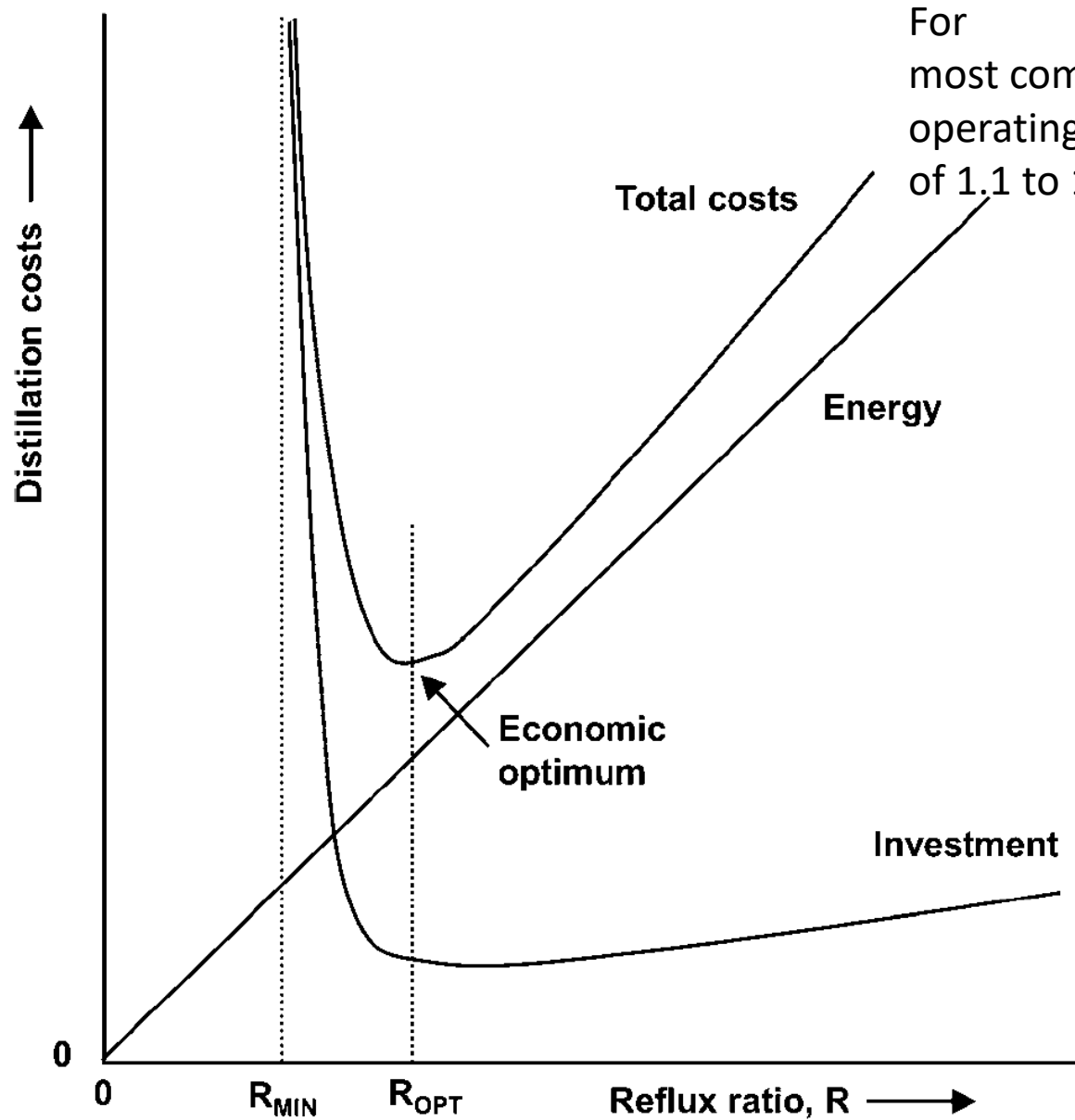
McCabe-Thiele Analysis

Minimum # stages

vs. Minimum reflux ratio



McCabe-Thiele Analysis



For most commercial operations the optimal operating reflux ratios are in the range of 1.1 to 1.5 times the minimum reflux ratio.

Operational cost

McCabe-Thiele Analysis

$$R_{\min} = \left(\frac{L'}{D} \right)_{\min} = \left(\frac{L'}{V' - L'} \right)_{\min} = \frac{\left(\frac{L'}{V'} \right)_{\min}}{1 - \left(\frac{L'}{V'} \right)_{\min}}$$

For most commercial operations the optimal operating reflux ratios are in the range of 1.1 to 1.5 times the minimum reflux ratio.

Operational cost

McCabe-Thiele Analysis

One question raised in the revision section – *how does one determine the optimal location of the feed stage?*
 In the following example, both the distillation and condensation stages are analyzed, and one sees how to find the stage for the initial (specified) composition.

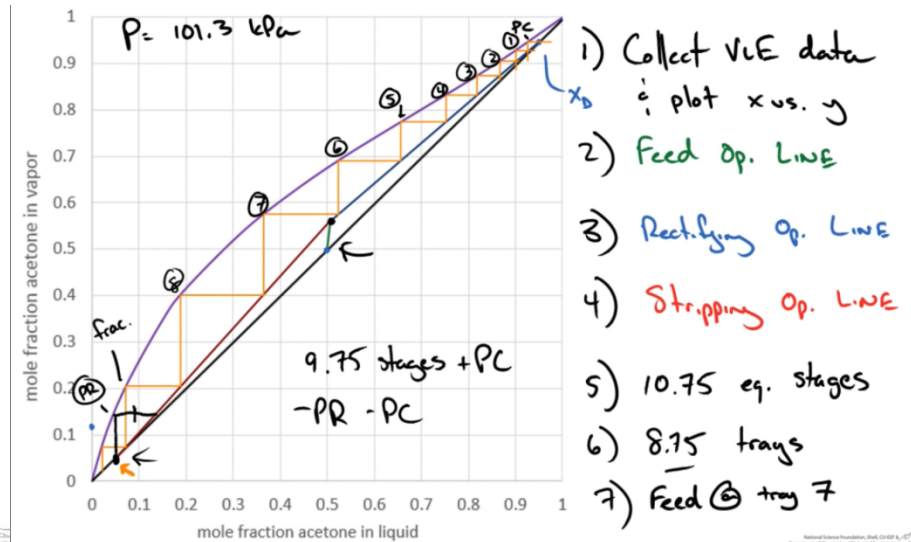
<https://youtu.be/OPFVXqLxNF0?t=128> and more detailed examples:

Distillation Column Example Using the McCabe-Thiele Method

Acetone and ethanol are separated using a distillation column with a partial condenser and partial reboiler. An equimolar, sub-cooled liquid feed enters at 100 kmol/hr and condenses 1 mole of vapor for every 6 moles of feed. The separation requires a distillate vapor that is 95 mol% acetone and bottoms liquid that is 5 mol% acetone. The reflux is returned from the condenser to the column as a saturated liquid and the operation is run at $(L/V) = 1.4 * (L/V)_{min}$. Assume constant molar overflow conditions.

Perform the following:

- Plot the operating lines for the rectifying and stripping sections and the feed line.
- Determine the number of equilibrium stages required and number of trays if each tray has an efficiency of 1.
- Determine the optimal feed location.
- Determine the molar flow rates in and out of the condenser (V and D) and boiler (L and B).

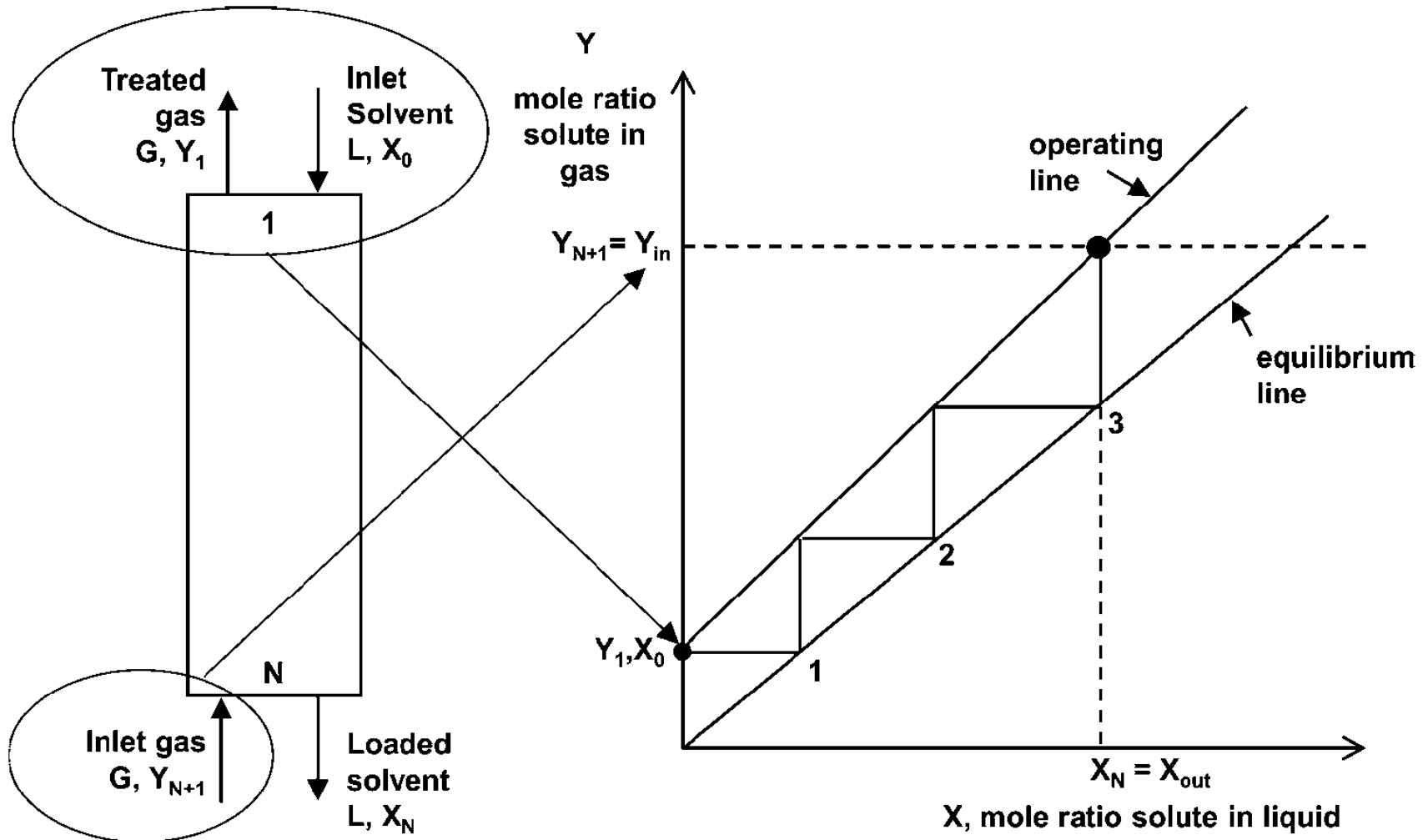


<https://youtu.be/Cv4KjY2BJTA?t=7>

See how after finding the two operation lines
 One finds the feed location is in stage 7.

<https://youtu.be/eIjk5uXmBRc?t=190>

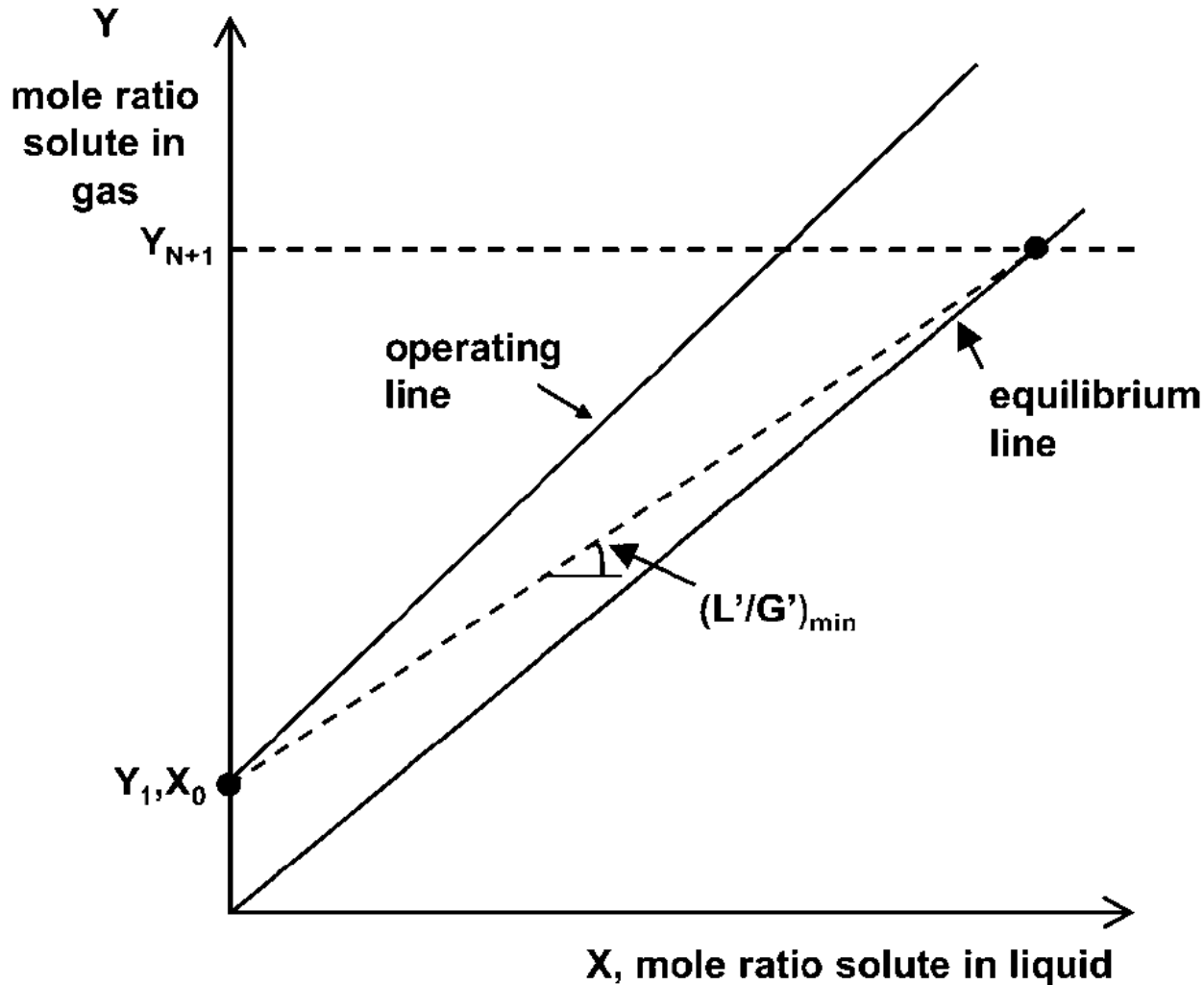
Operating Lines for Absorption



McCabe-Thiele diagram for absorption

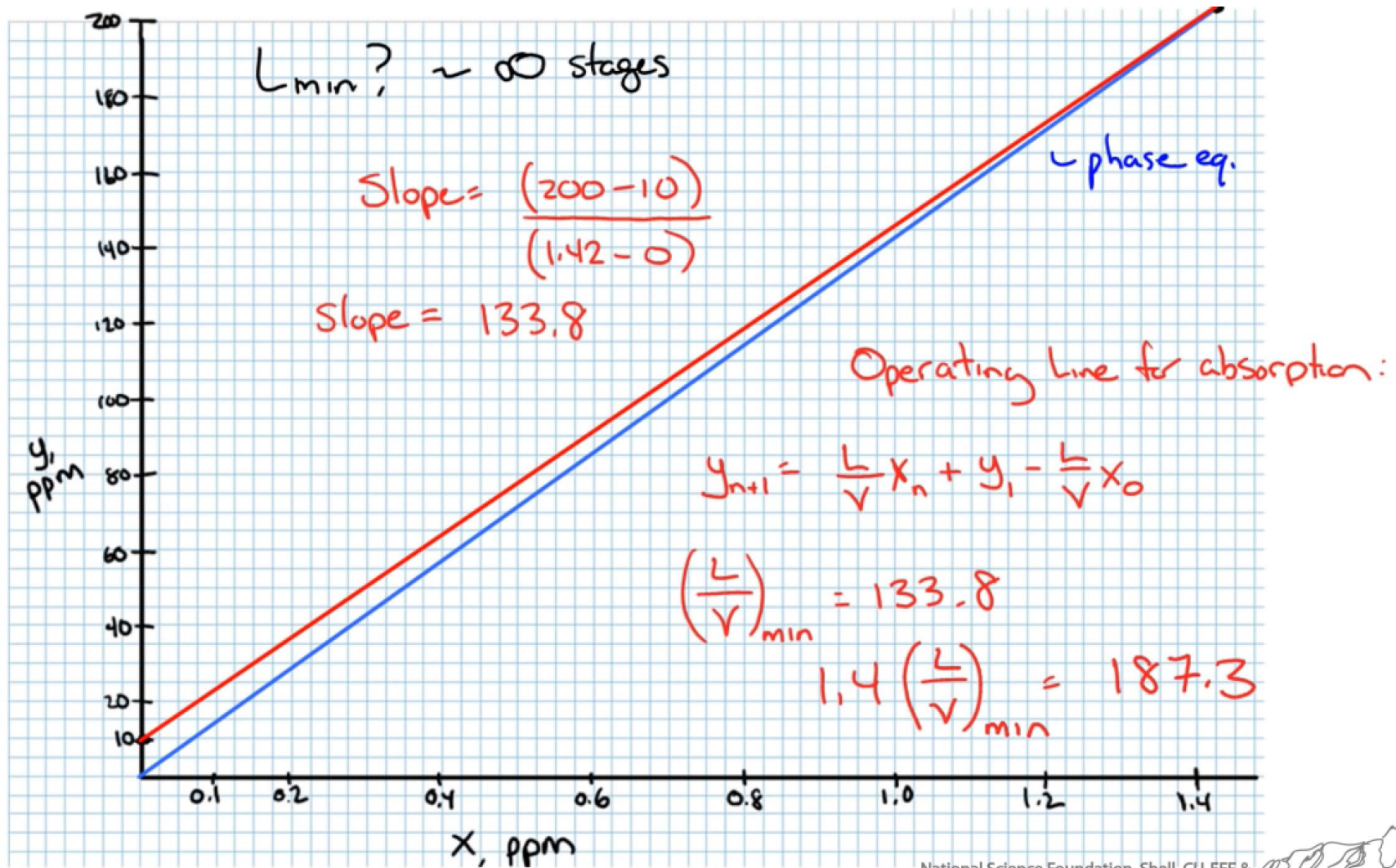
operating line in absorption is above the equilibrium line

Absorption and Stripping



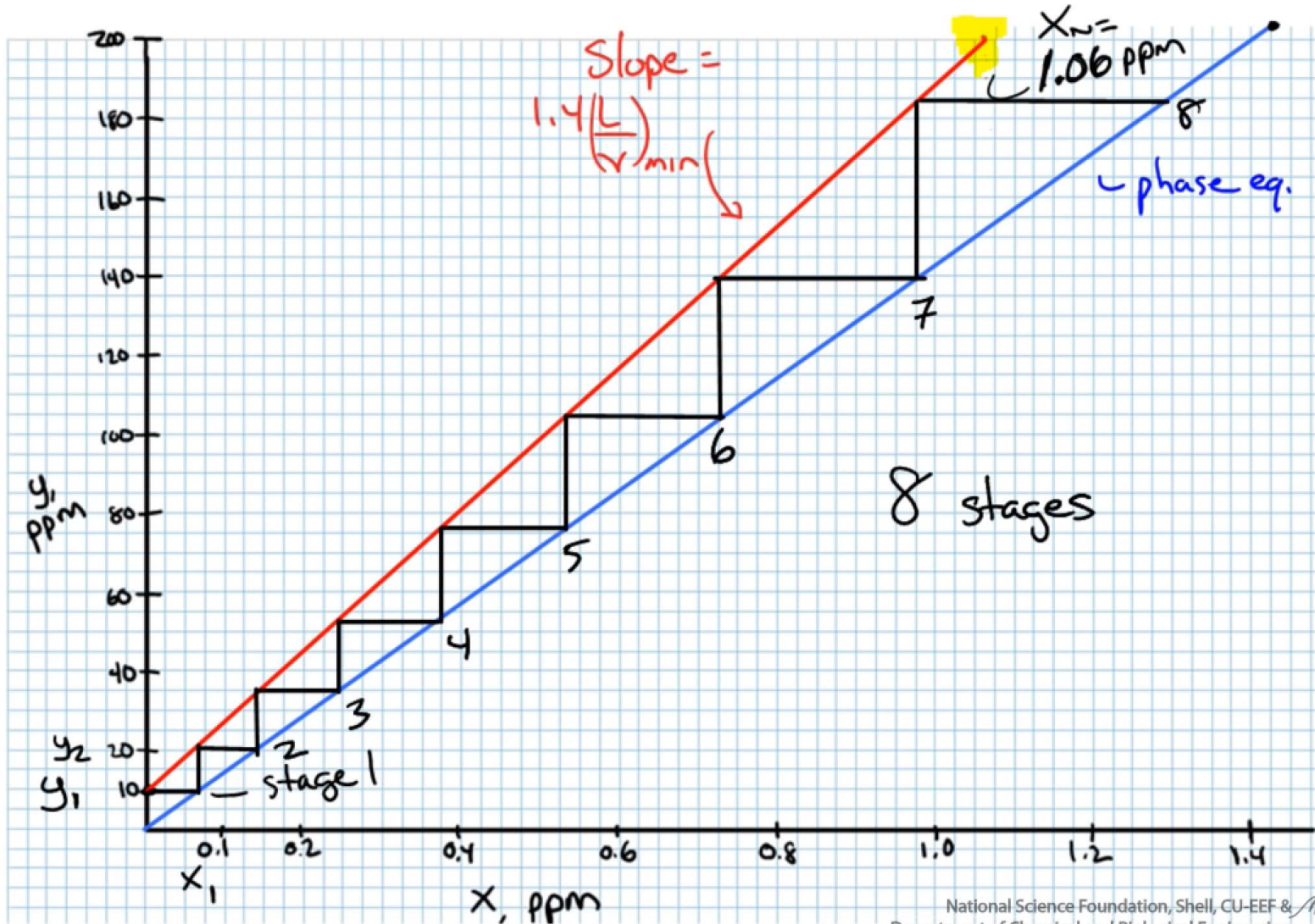
McCabe-Thiele diagram for minimum L/G ratio for absorption

Absorption and Stripping



McCabe-Thiele diagram for minimum L/G ratio for absorption

Absorption and Stripping



McCabe-Thiele diagram for minimum L/G ratio for absorption

Absorption – Note in example:

You won't need to determine # variables or DOF,

ASSUMPTIONS:

- Each stage operates adiabatically and approximately at 1.5 atm
= 2N variables fixed
- Entering liquid @ 25°C
DOF = SHORT 1 VARIABLE
- $L' = 1.4 L_{min}$ [Bellport range $1.1 L_{min} < L' < 2 L_{min}$]
- Total flow rates L and V are constant (Dilute solutions)
- Y, X (mole ratios) = y, x (Plot mole fractions, ppm)

National Science Foundation, Shell, CU-EEF & Department of Chemical and Biological Engineering University of Colorado Boulder

<https://youtu.be/BoPKngZZwVI?t=317>

- Total flow rates L and V are constant (Dilute solutions)
- Y, X (mole ratios) = y, x (Plot mole fractions, ppm)

LOOK UP:

- HENRY'S LAW CONSTANT: 211.19 atm/mole fraction in water (25°C, 1 atm)

PHASE Equilibrium Line:

$$y = \frac{Hx}{P}$$

Start at this timepoint with Henry's law

And try to solve the problem.

<https://youtu.be/BoPKngZZwVI?t=349>

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The example is done step-by-step in detail also graphically, and you see a lot of the correspondences with the McCabe-Thiely analysis for distillation.

How Long Does a Filter Last?

<https://www.thameswater.co.uk/help-and-advice/water-quality/check-the-water-quality-in-your-area>

Calculate life for a C150 filter **Hardness**

with 267 ppm water?

The water supplied in the MILE END zone is HARD water.

Calcium carbonate(CaCO₃): 267 ppm

PURITY C Finest	C150	C500	
Technology	softening		
Capacity ¹ with a total hardness of 10 °dH and 0 % bypass ²	1.100 l	3.414 l	
Max. operating pressure	8,6 bar		
Water intake temperature	4 – 30 °C		
Flow at 1 bar pressure loss	145 l/h	140 l/h	
Nominal flow	60 l/h		100 l/h
Pressure loss at nominal flow	0.25 bar		0.5 bar
Dimensions (W/D/H) Filter head with filter cartridge	117/104/419 mm	144/144/557 mm	
Weight (dry/wet)	1.8/2.8 kg	4.6/6.9 kg	

10 dH = 178 ppm, so Capacity = 1100 L * 178 mg/L = 196g CaCO₃
 so x = 196 g / 267 mg/L = 734 L And it costs £74

So £74 / 734 L = £0.10 / L – for good tasting and no-scale water

If it cleans molecular ions, does it also filter bacteria and viruses?

Osmotic Pressure

Osmotic pressure determined for different salts:

<https://youtu.be/AGRjXcB14qA?list=PL61BFC1C064B40049&t=31>

An osmotic shock disruption process was determined to require less than 0.01 M NaCl to disrupt cells which contain salt roughly equivalent (in osmotic terms) to 0.1 M NaCl at 25C. To improve downstream processing, the disruption system will be changed to use MgCl₂ instead of the NaCl. Estimate the required concentration of MgCl₂ to effectively lyse the cells at 25C.

**See if you can first solve the problem yourself,
Then continue the video to see the solution if you need to.**

Drying –

Terminology and Learning Goals

By the end of this lecture you'll be able to: **drying**. (how prosaic!) Yet, in a quantitative way in which none of your friends outside this class would be able to.

Say what are **wet-bulb temperature, absolute humidity, relative humidity**, .
Other vocabulary: **Chilton-Colburn transfer numbers for heat and mass**,
See this concise summary: https://www.youtube.com/watch?v=7YIQ_4jL_gs

We'll identify **Drying Mechanisms** and

Derive **simplified rate equations** to estimate drying times

Discuss **Drying Methods** and **Drying Equipment**

Applications in: Foods, building materials, powders, papers, fabrics

Discuss Efficiency and cost –

Drying vs. unnecessary transportation of products containing water

Bread Rusk and Hair Drying



Need to strike an optimum balance between
Temperature and Drying Rate

Drying – Wet Bulb Temperature

When the amount of air \gg amount of evaporated moisture

The dynamic equilibrium (non-equilibrium steady state)

Temperature of a wet surface is called T_{wb} , the wet-bulb temperature

$$\Phi_{vap} \cdot \Delta H_{vap} = h (T_f - T_{wb}) \quad \text{units [J s}^{-1} \text{ m}^{-2}\text{]}$$

Drying rate *Energy transfer*
Energy *from the surface*

where

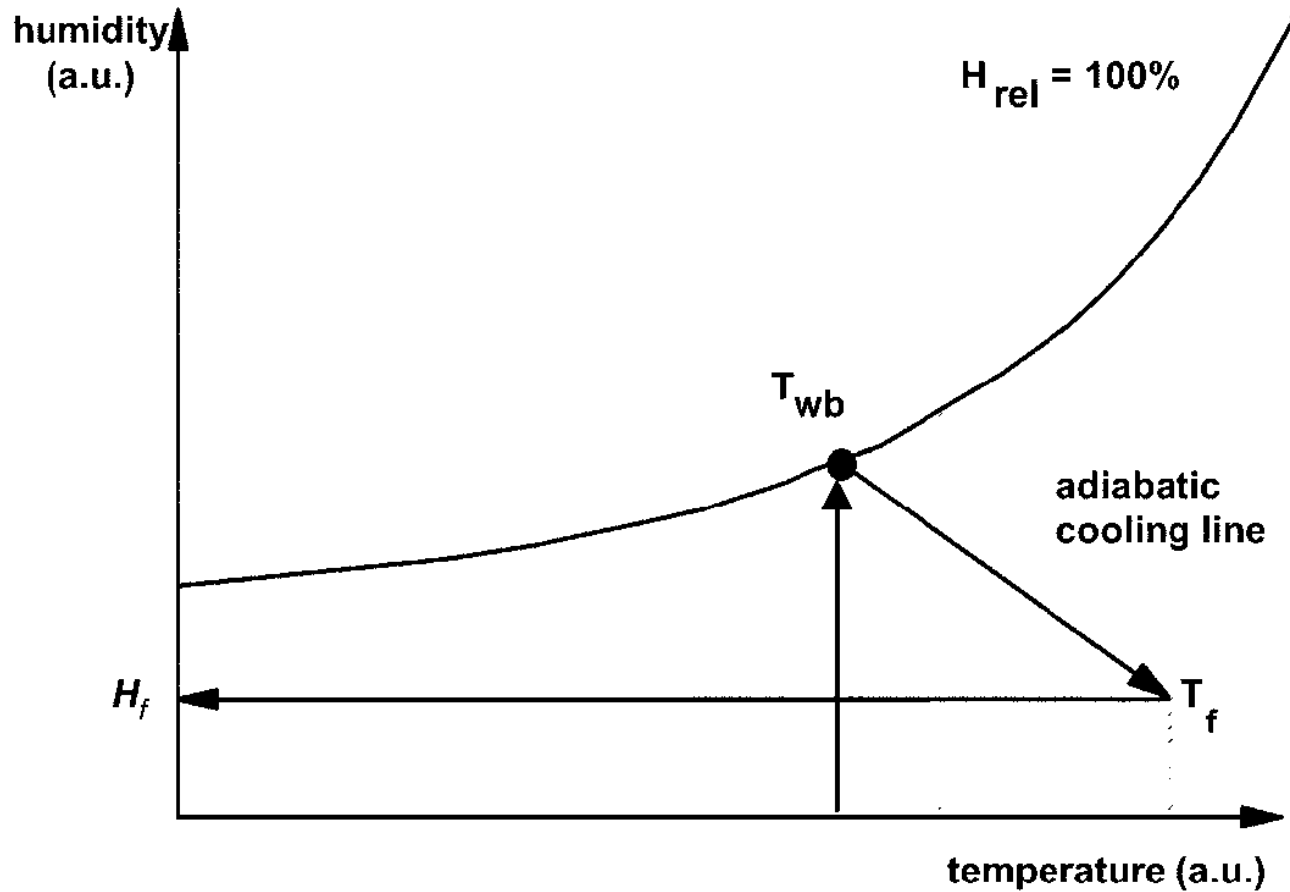
h = heat transfer coefficient (convection) [$\text{W m}^{-2} \text{K}^{-1}$]

ΔH_{vap} = molar heat of evaporation [K]

Examples – Passive cooling in non-glazed pottery

T_{wb} indicates max amount of vapor that can be carried the dry gas

Air Humidity – From Wet-Bulb Temp.



Relating Wet and Dry-bulb temperatures – via adiabatic cooling lines

Psychrometric Chart

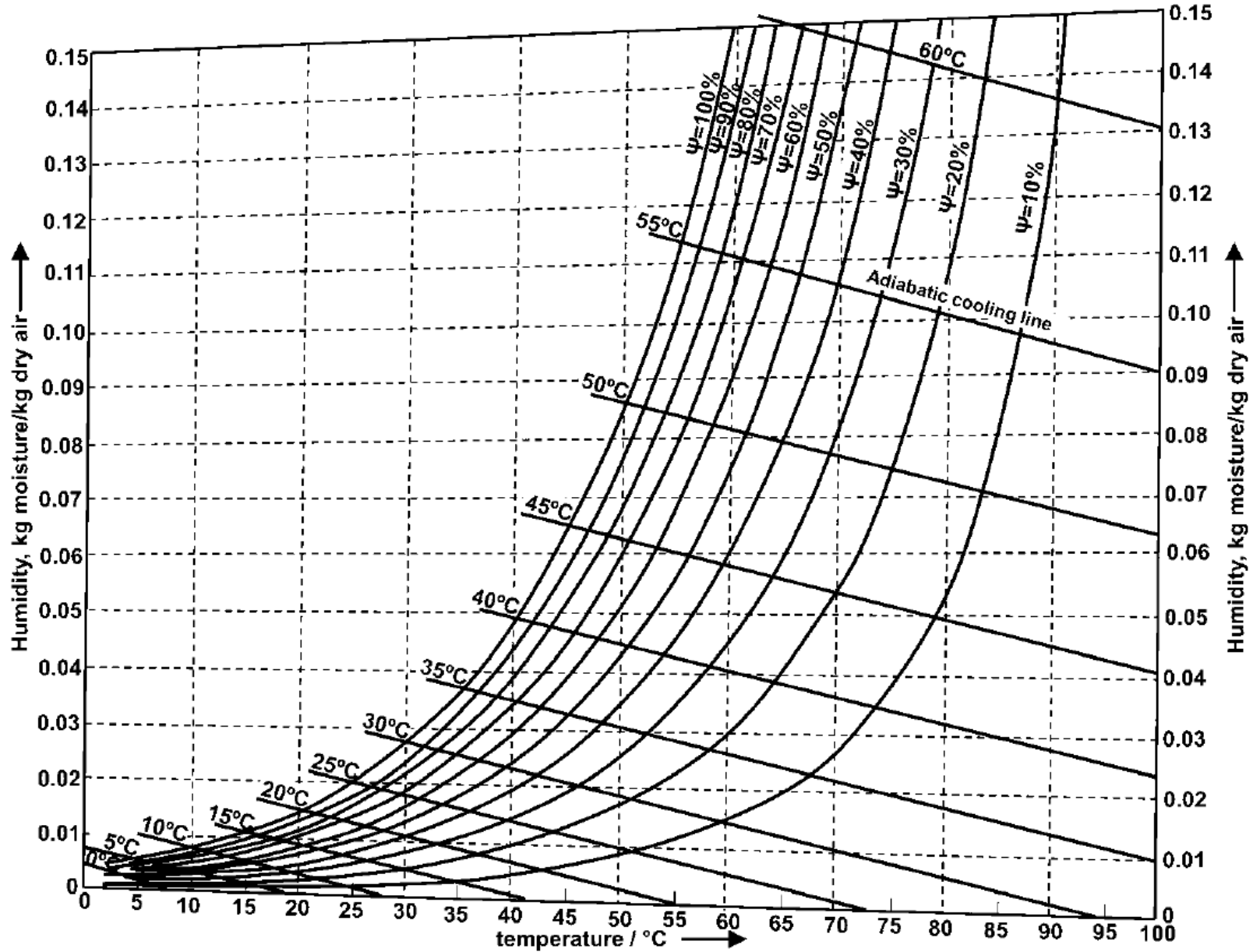
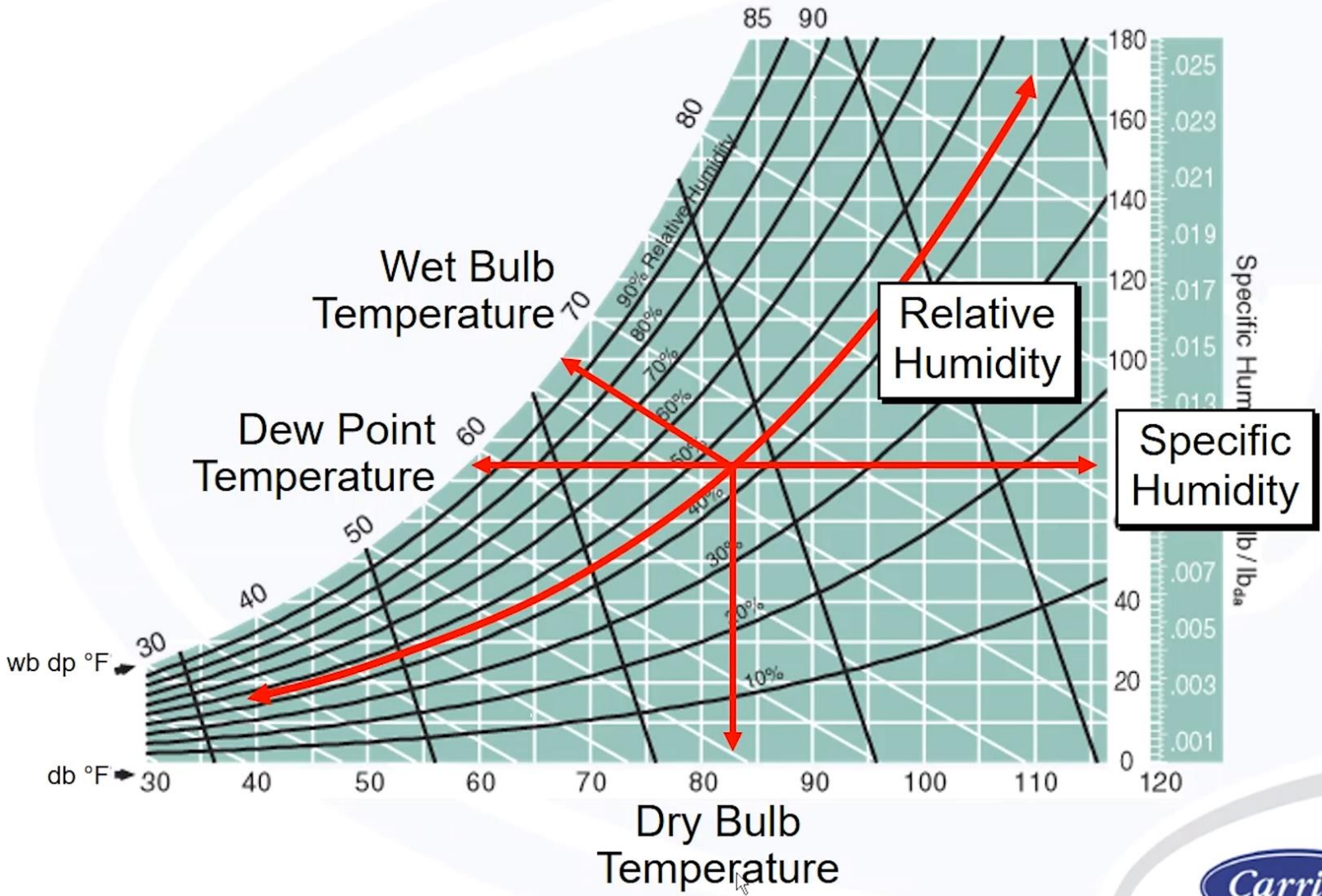


Fig. 7.3 Psychrometric chart of air-water at 1 bar total pressure (adapted from [56]).

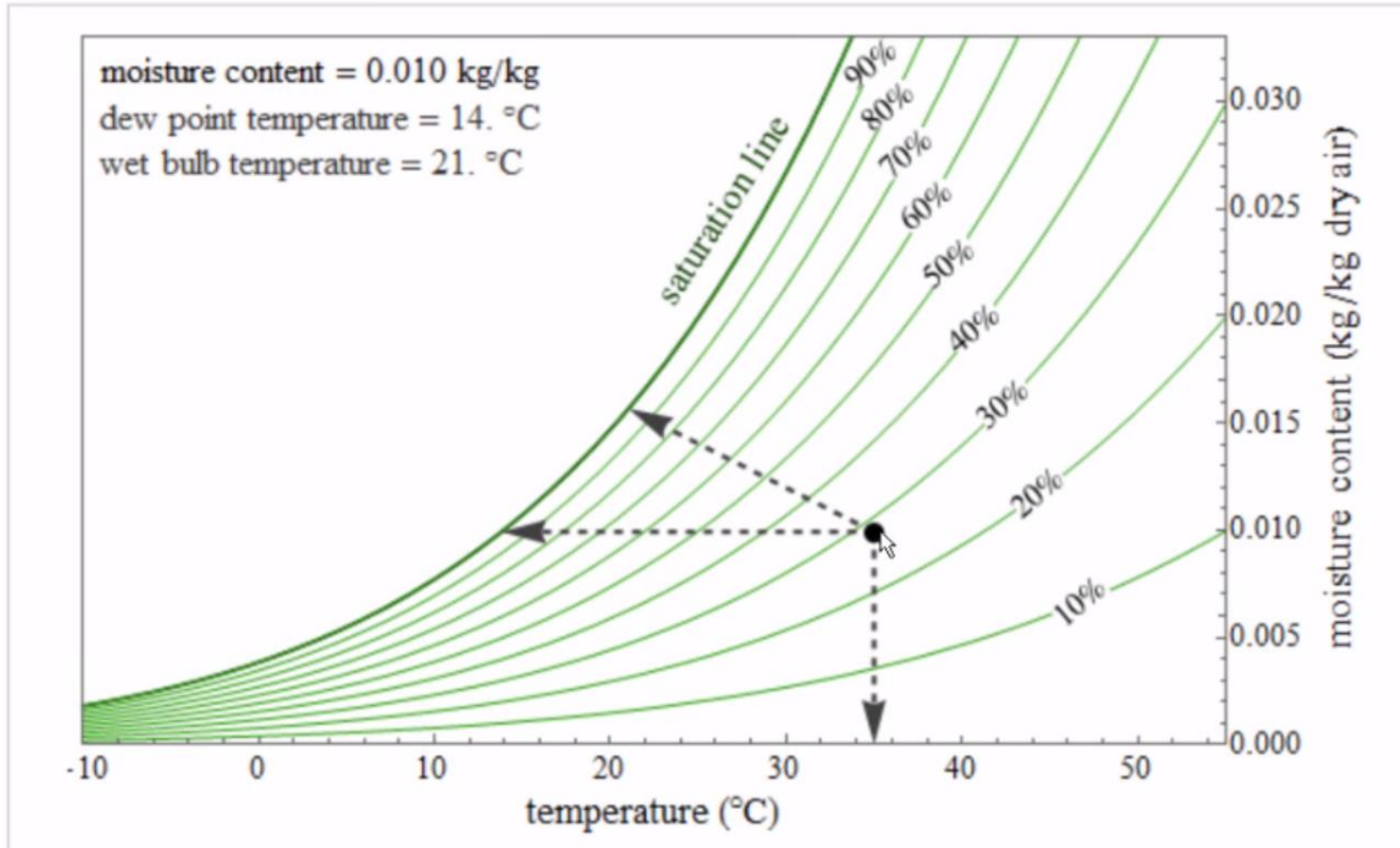
Properties of Air - Psychrometric Chart



Psychrometric Chart - Interactive

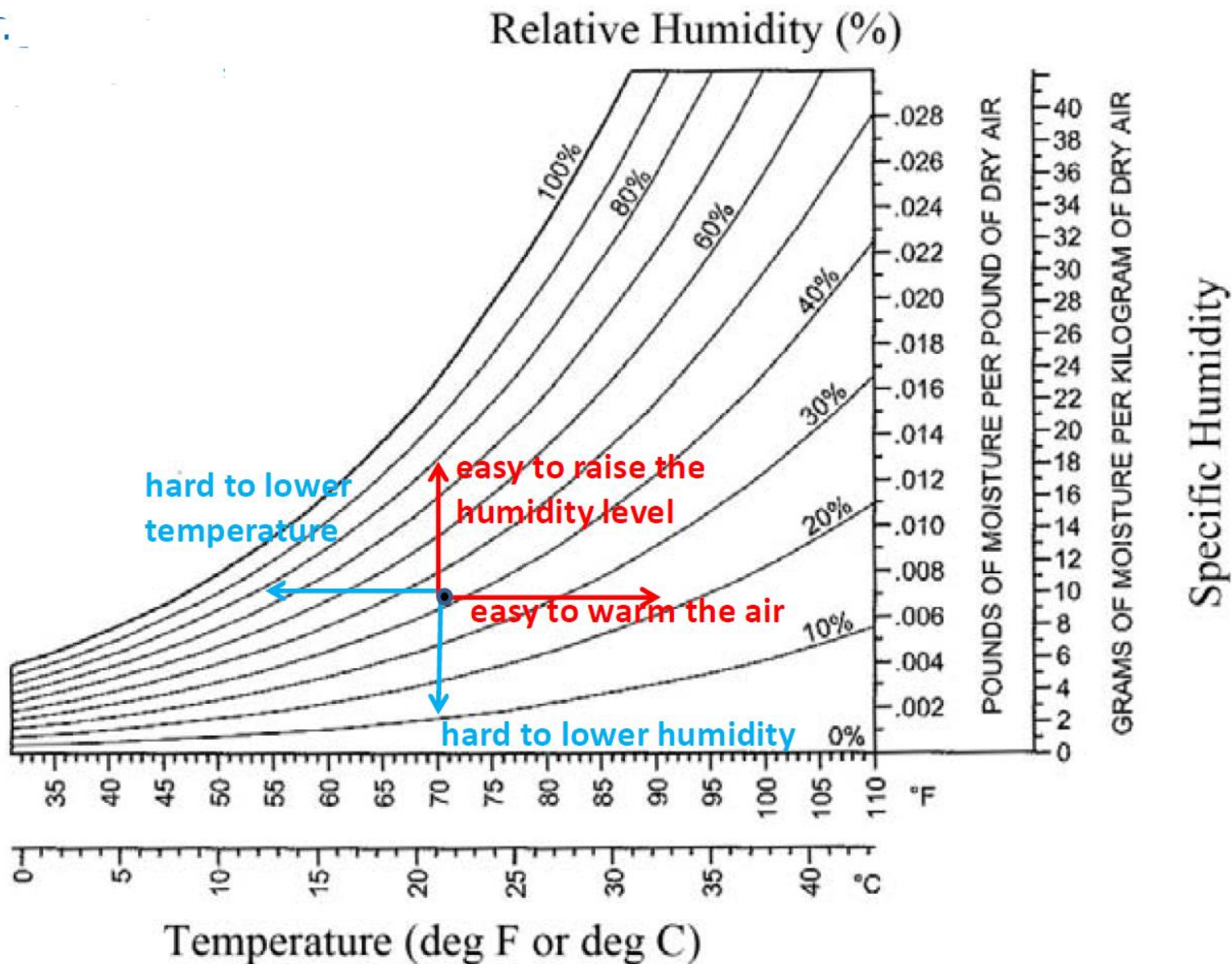
relative humidity enthalpy specific volume temperatures grid lines
display values

relative humidity (%) dry bulb temperature (°C)



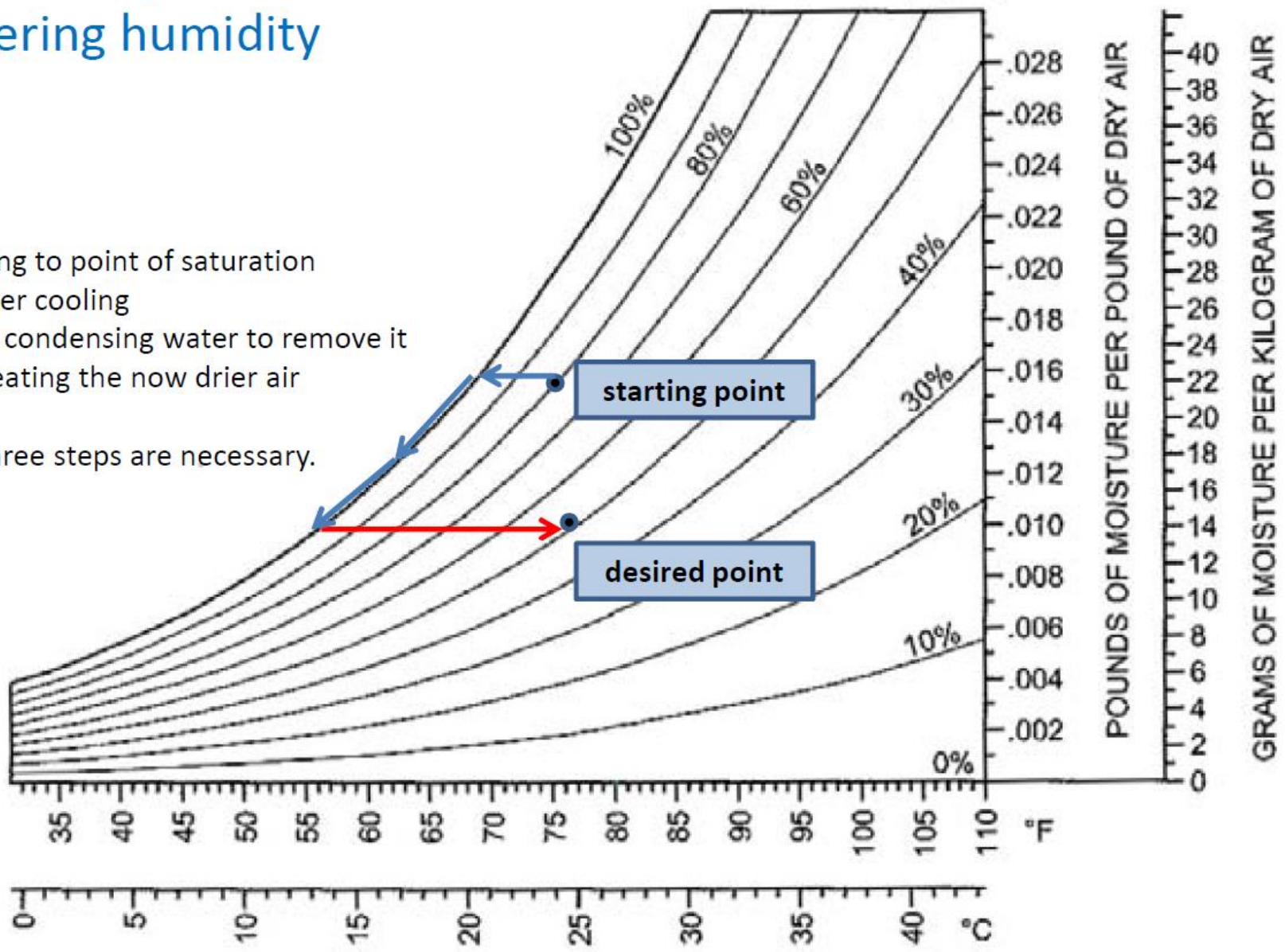
<https://youtu.be/IVwniWExPgA?t=207>

Psychrometric Chart - Practice



Typical way of lowering humidity

Relative Humidity (%)



- 1. Cooling to point of saturation
 - 2. Further cooling while condensing water to remove it
 - 3. Re-heating the now drier air
- Thus, three steps are necessary.

Specific Humidity

Saturation Vapor Pressure of Water

Experimental data taken from Dortmund Data Bank

Vapor Pressure of Water

The Tetens equation

$$P = 0.61078 \exp\left(\frac{17.27T}{T + 237.3}\right),$$

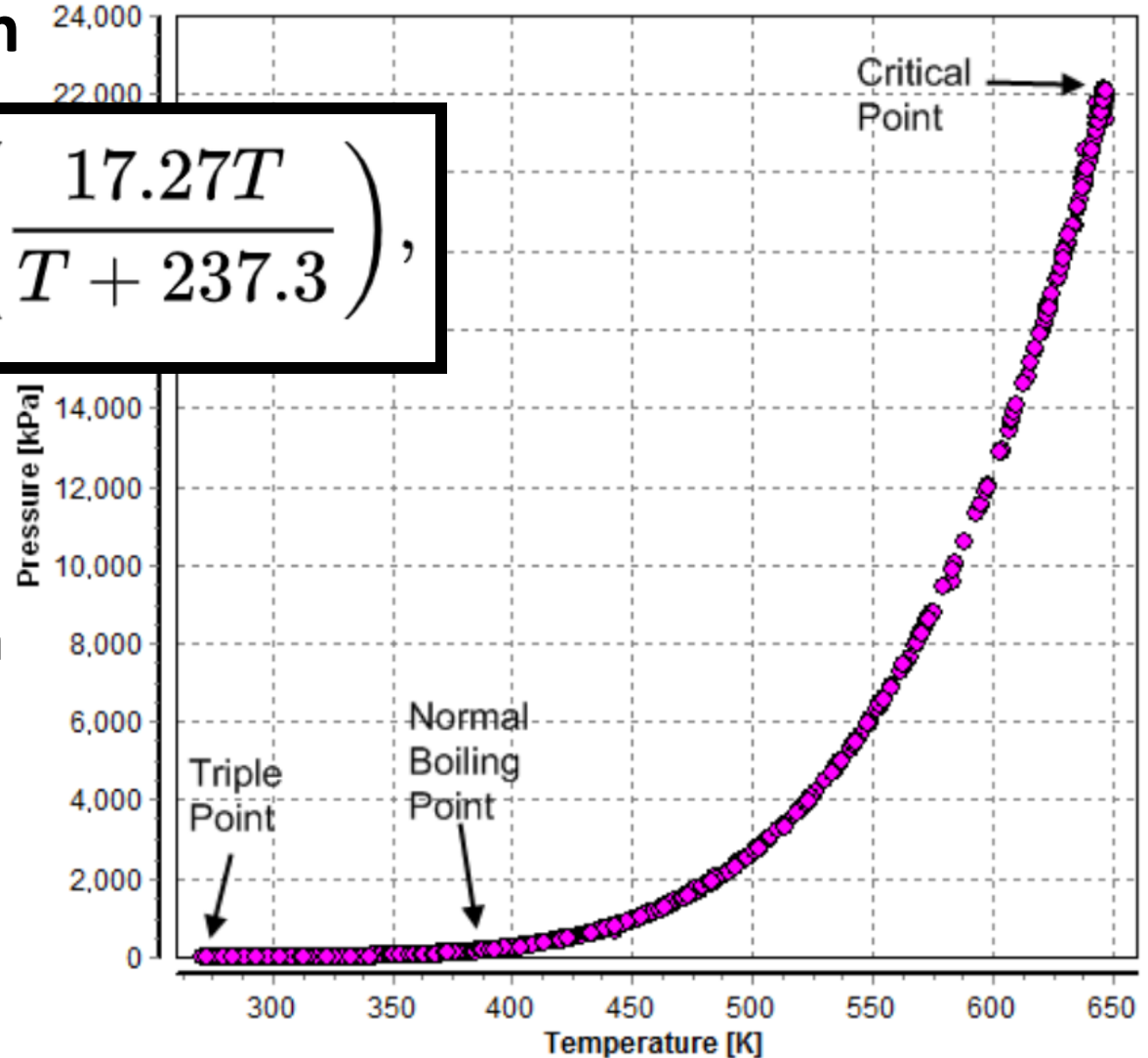
where

T = temperature in °C

and P = pressure in kPa

Above form valid for

$T > 0$ °C



Drying – Slowly at Low Vapor Pressures

For low drying rates, and low vapor concentrations c , drying rate Φ_{vap} is proportional to the driving force $(c_{sat(T_s)} - c_f)$



$$\text{Drying rate } \Phi_{vap} = k_g (c_{sat(T_s)} - c_f)$$

units $[\text{mol s}^{-1} \text{ m}^{-2}]$

where

T_f = temperature of heated air (with concentration c_f)

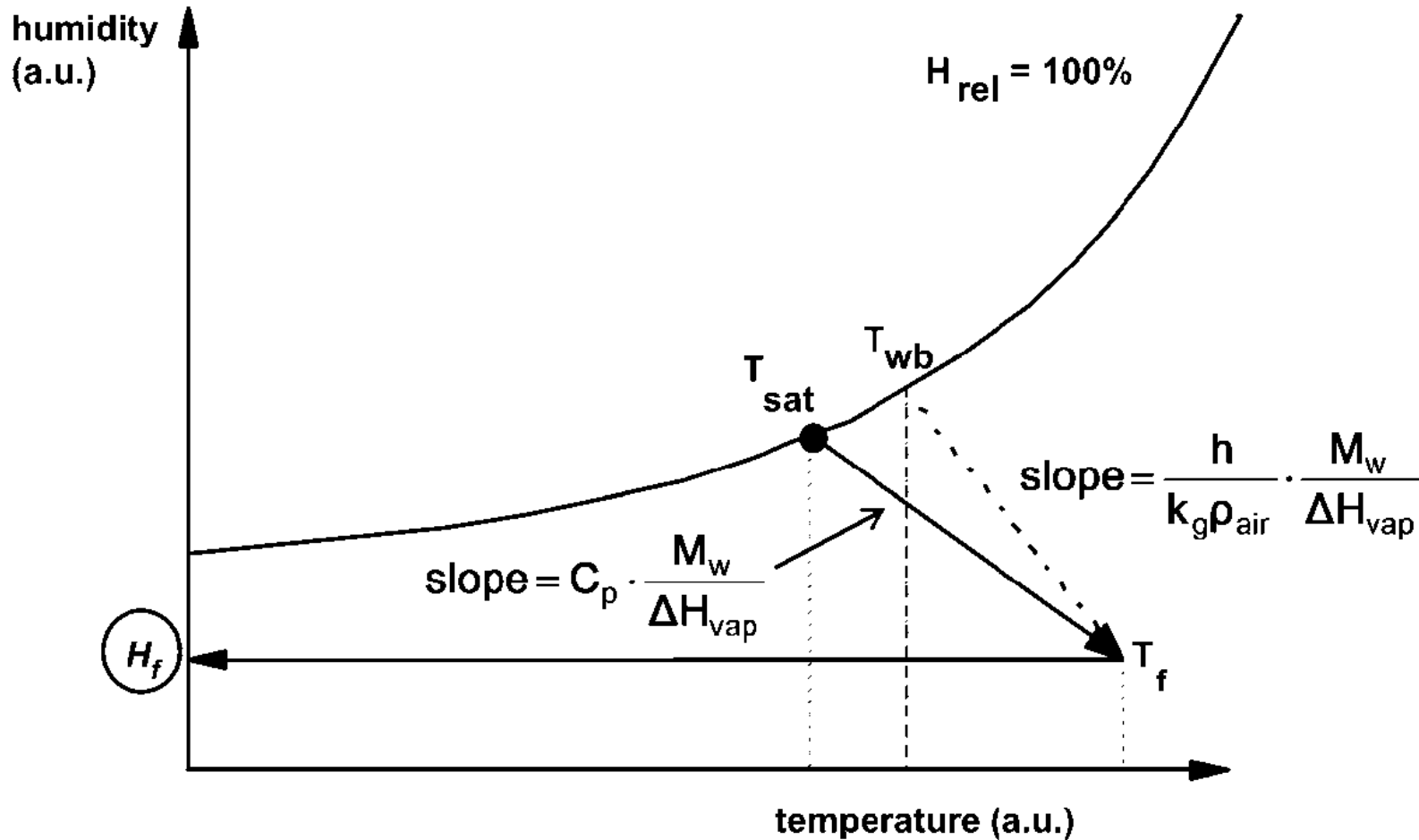
T_s = temperature of wet surface [K]

c_{sat} = saturation vapor (water) concentration at T_s $[\text{mol m}^{-3}]$

c_f = vapor (water) concentration in *feed* gas (air) $[\text{mol m}^{-3}]$

k_g = mass transfer coefficient $[\text{m s}^{-1}]$

Air Humidity – From Wet-Bulb Temp.



When stream of air Φ_{air} at T_f is mixed thoroughly and adiabatically, with liquid at T_{sat} , it leaves completely saturated with vapors (@ T_{sat})

Drying – Wet Bulb Temperature

When the amount of air \gg amount of evaporated moisture

The dynamic equilibrium (non-equilibrium steady state)

Temperature of a wet surface is called T_{wb} , the **wet-bulb temperature**

$$\Phi_{vap} \cdot \Delta H_{vap} = h (T_f - T_{wb}) \quad \text{units [J s}^{-1} \text{ m}^{-2}\text{]}$$

Drying rate *Energy transfer*
Energy *from the surface*

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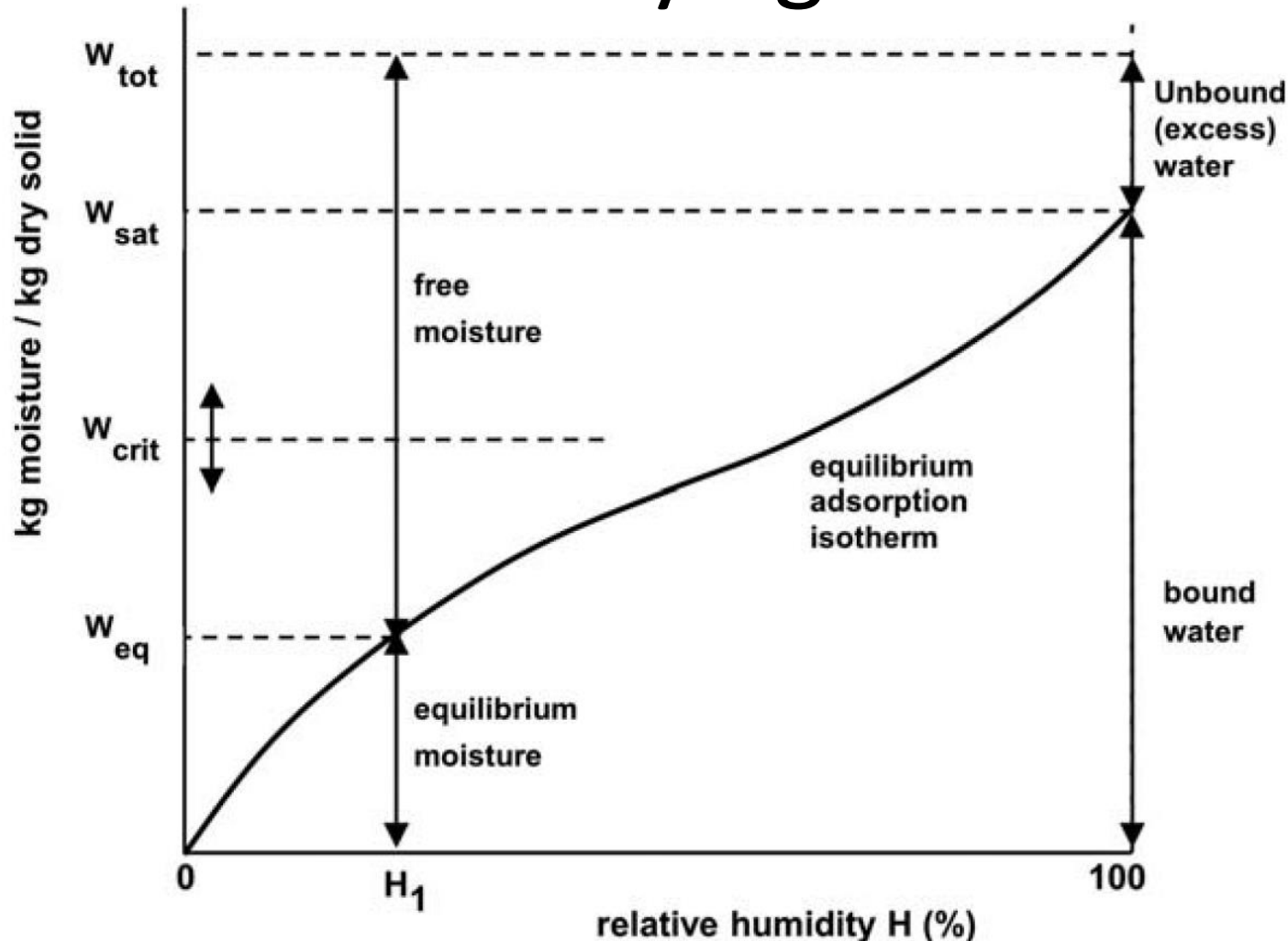
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ΔH_{vap} = molar heat of evaporation [K]

Examples – Passive cooling in non-glazed pottery

T_{wb} indicates max amount of vapor that can be carried the dry gas

Drying Solids



*Unbound
vs.
Free
Moisture*

*Bound/Unbound Water and Structure of the solid
– lead to different drying regimes and mechanisms*

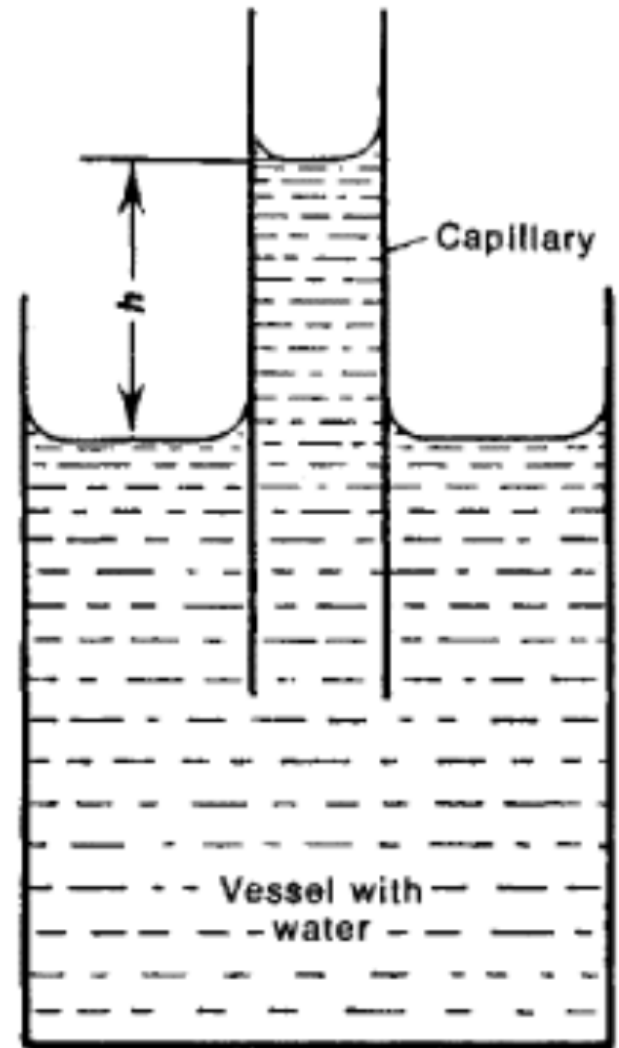
Drying Solids – Water in Pores

$$p_{sat} = p_{sat}^{\infty} \exp \frac{V_{liq} (P_{liq} - P)}{RT}$$

where V_{liq} = molar volume of liquid.

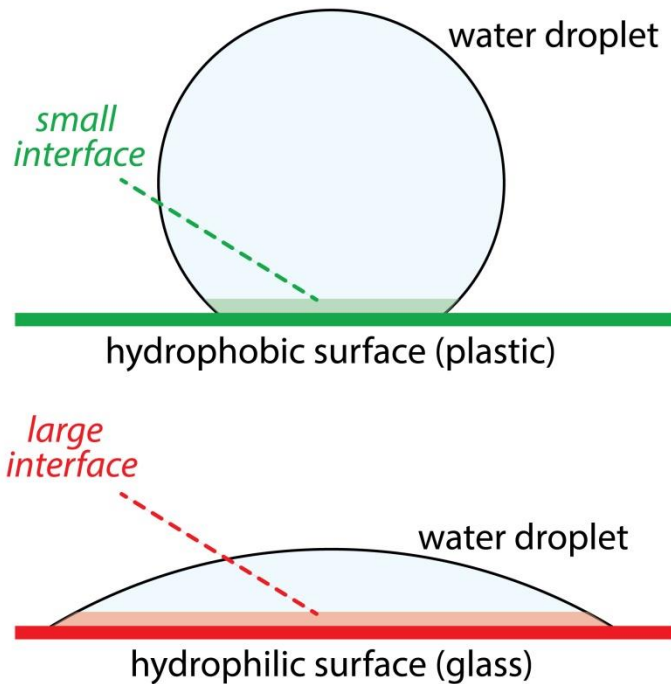
Pressure in the liquid can affect pressure above it

$$P_{liq} - P = \gamma \left(\frac{1}{r_1} + \frac{1}{r_2} \right)$$

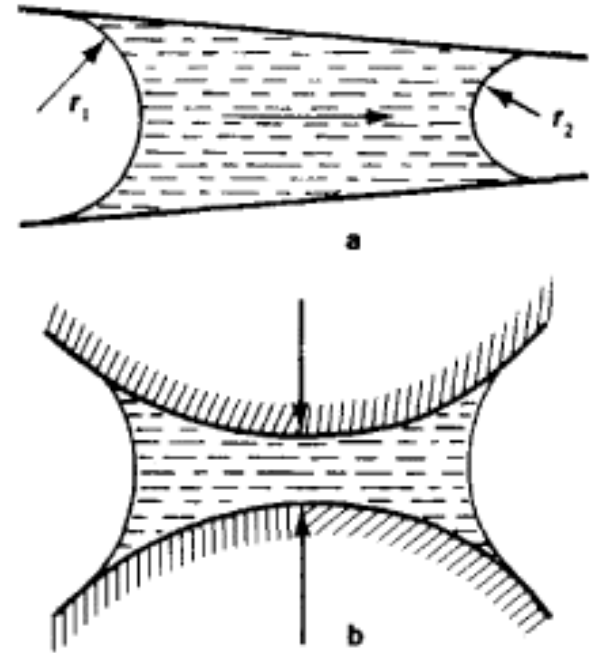


Pressure in curved geometries – from Laplace Eqn.

Pressure in Droplets vs Bubbles

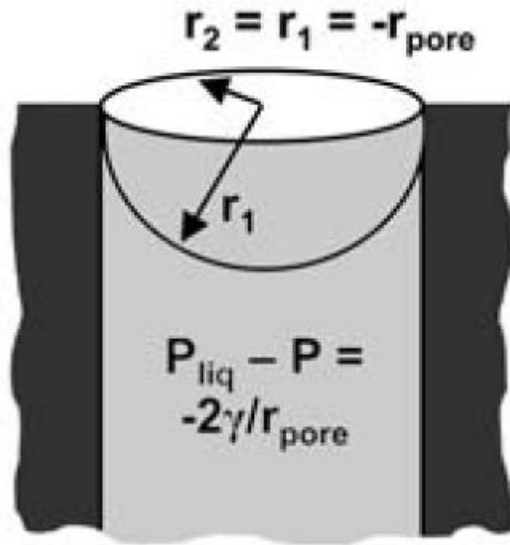


$$\Delta P = \gamma \left(\frac{1}{r_1} + \frac{1}{r_2} \right)$$



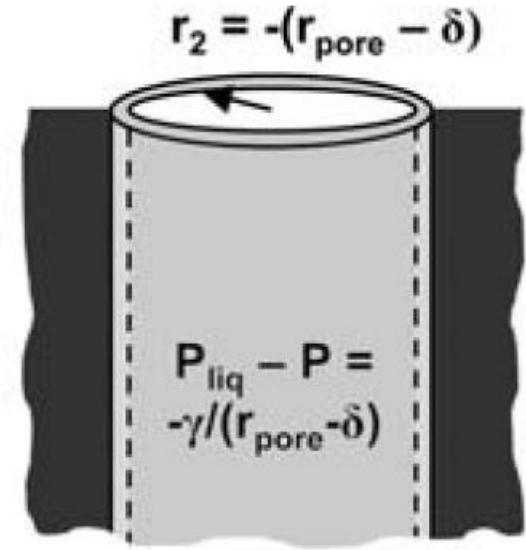
Pressure in curved geometries – from Laplace Eqn.

Pressure in Bubbles and Pores



$$p_{\text{sat}} = p_{\text{sat}}^{\infty} \exp\left(-\frac{V_{\text{liq}}}{RT} \frac{2\gamma}{r_{\text{pore}}}\right)$$

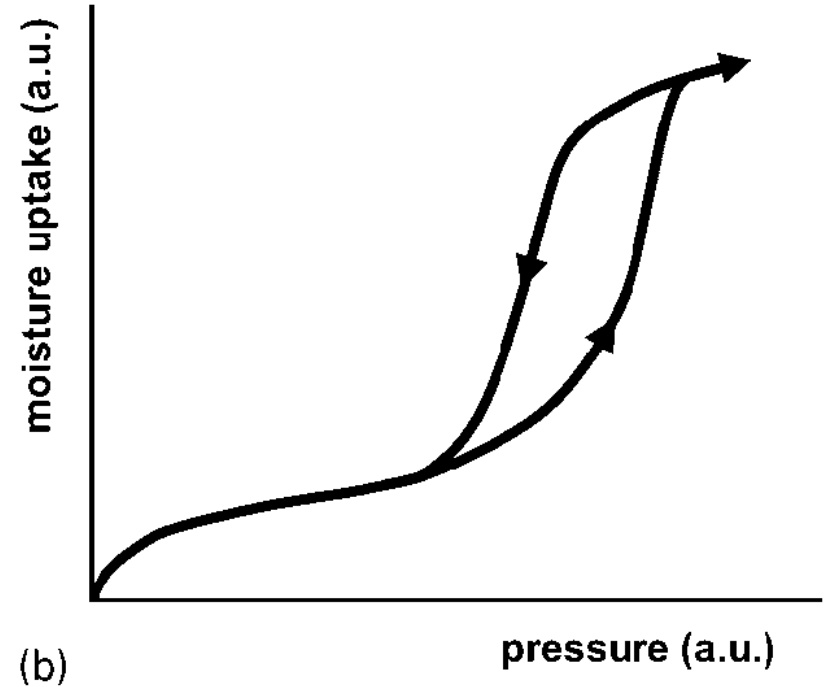
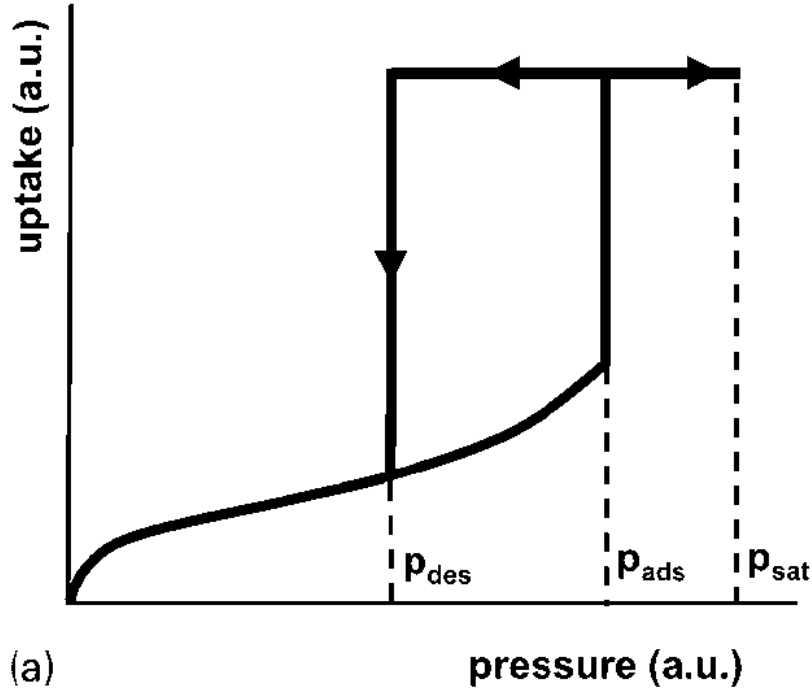
Pressure to empty pore



$$p_{\text{sat}} = p_{\text{sat}}^{\infty} \exp\left(-\frac{V_{\text{liq}}}{RT} \frac{\gamma}{r_{\text{pore}} - \delta}\right)$$

Pressure to Fill pore

Drying Porous Solids



Ideal Cylinder Pores

Irregular Pores

Adsorption/ desorption hysteresis