

$$K = \underbrace{x_1}_{\text{weight}} D + \frac{x_2}{\alpha} V + \frac{x_3}{\alpha} B$$

$$\begin{aligned} \text{Cov}(K, D) &= \text{Cov}(x_1 D + x_2 V + x_3 B, D) \\ &= x_1 \overbrace{\text{Cov}(D, D)}^{\text{Var } D} + x_2 \text{Cov}(V, D) + x_3 \text{Cov}(B, D) \end{aligned}$$

$$E(R_j) = r + \beta_j (E(R_k) - r)$$

\Leftrightarrow

$$\beta_j = \frac{\sigma_{jk}}{\sigma_k^2}$$

$$\frac{E(R_j) - r}{\sigma_{jk}} = \frac{E(R_k) - r}{\sigma_k^2}$$

constant

one tangency portfolio!

$$\sigma_{jk} = \text{Cov}(j, k) = \alpha [E(R_j) - r]$$

β, D, V, B ; system of 4 eq and 4 unknowns