

## Cox PH Seminar Question – Solution

(i) the baseline hazard  $h_0$  is where all  $z_i = 0$

so in this case that is a female patient where the existing treatment is applied immediately on diagnosis

(ii) here  $z_1 = 6/12 = 0.5$ ,  $z_2 = 1$ ,  $z_3 = 1$

(a) therefore  $h(t) = h_0 \exp[0.5 \times 0.5 + 0.01 \times 1 - 0.05 \times 1] = h_0 \exp[0.21]$

(b) the survival function is

$$S(t) = \exp\left[-\int_0^t h(s) ds\right]$$

$$\text{from (a) above } S(t) = \exp\left[-\int_0^t h_0 \exp[0.21] ds\right]$$

$$= \exp\left[-\exp[0.21] \int_0^t h_0 ds\right]$$

$$\text{so } S(t) = \exp\left[-\int_0^t h_0 ds\right] \exp[0.21]$$

(iii) for this female patient,  $z_1 = 0$ ,  $z_2 = 1$ ,  $z_3 = 0$

so  $h(t) = h_0 \exp[0.5 \times 0 + 0.01 \times 1 - 0.05 \times 0] = h_0 \exp[0.01]$

we are given  $S(5) = 0.75$

$$\text{from (ii)(b) we know } S(5) = \exp\left[-\int_0^5 h_0 ds\right] \exp[0.01]$$

$$\text{which means that } \exp\left[-\int_0^5 h_0 ds\right] = 0.75 \exp[-0.01]$$

and then for the male patient

$$S(5) = \exp\left[-\int_0^5 h_0 ds\right] \exp[0.21] = (0.75 \exp[-0.01]) \exp[0.21]$$

$$S(5) = 0.7037$$