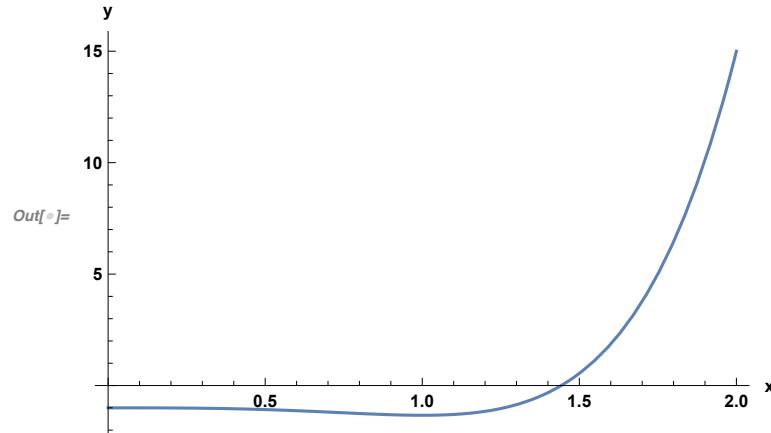


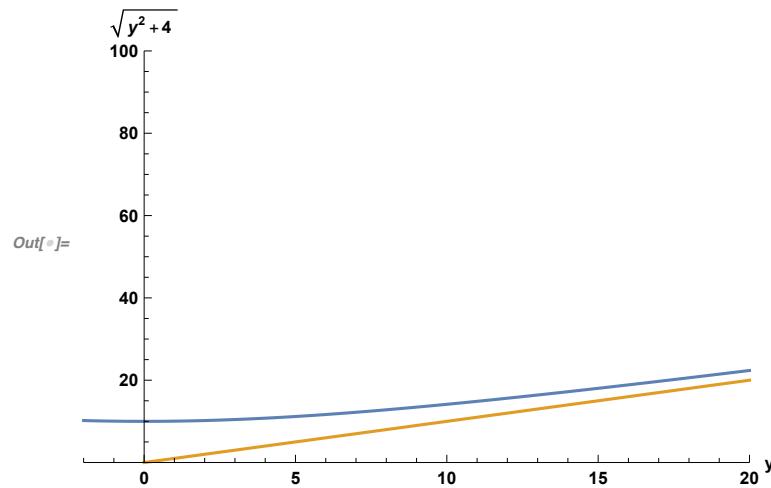
## Plot normal equations

e.g.  $y = \left( \frac{x^3}{3} - 1 \right) \left( x^3 + 1 \right)$

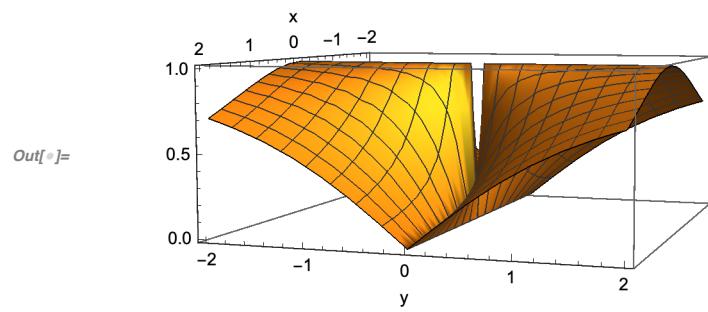
```
In[]:= Plot[(x^3/3 - 1) (x^3 + 1), {x, 0, 2}, PlotRange -> All, AxesLabel -> {"x", "y"}]
```



```
In[]:= Plot[{Sqrt[y^2 + 100], y}, {y, -2, 20}, PlotRange -> {{-2, 20}, {0, 100}}, AxesLabel -> {"y", "Sqrt[y^2 + 4]}]
```



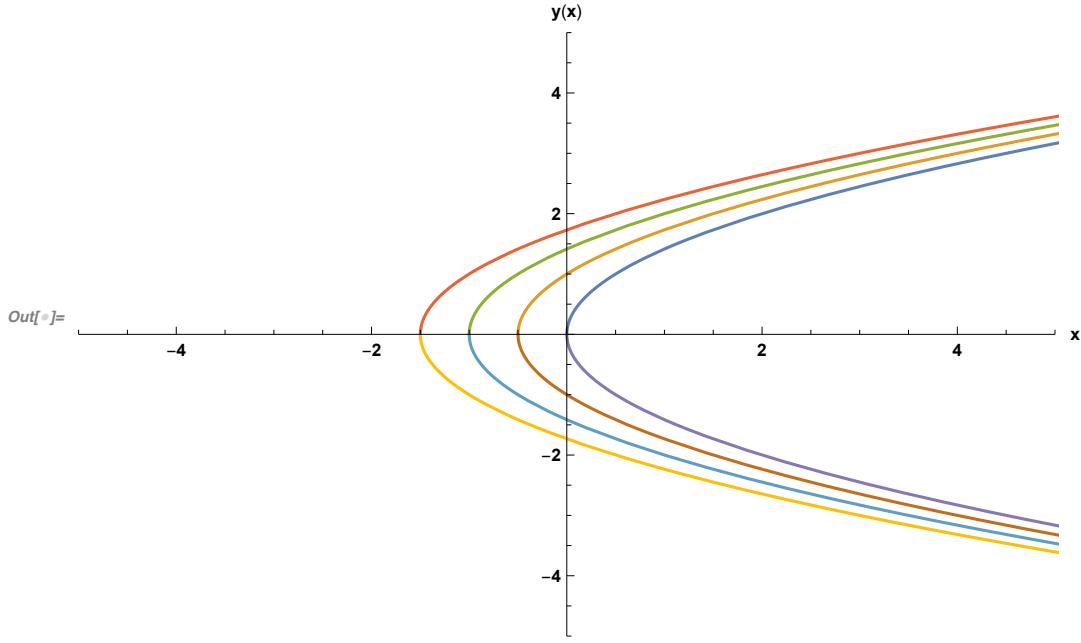
```
In[]:= Plot3D[Sqrt[y^2]/Sqrt[x^2 + y^2], {x, -2, 2}, {y, -2, 2}, PlotRange -> All, AxesLabel -> {"x", "y"}]
```



---

Plot the implicit solution e.g.  $y^2 = 2x + c$

```
In[6]:= Plot[{Sqrt[2 x], Sqrt[2 x + 1], Sqrt[2 x + 2], Sqrt[2 x + 3], -Sqrt[2 x], -Sqrt[2 x + 1], -Sqrt[2 x + 2], -Sqrt[2 x + 3]}, {x, -10, 10}, PlotRange → {{-5, 5}, {-5, 5}}, AxesLabel → {"x", "y(x)"}]
```



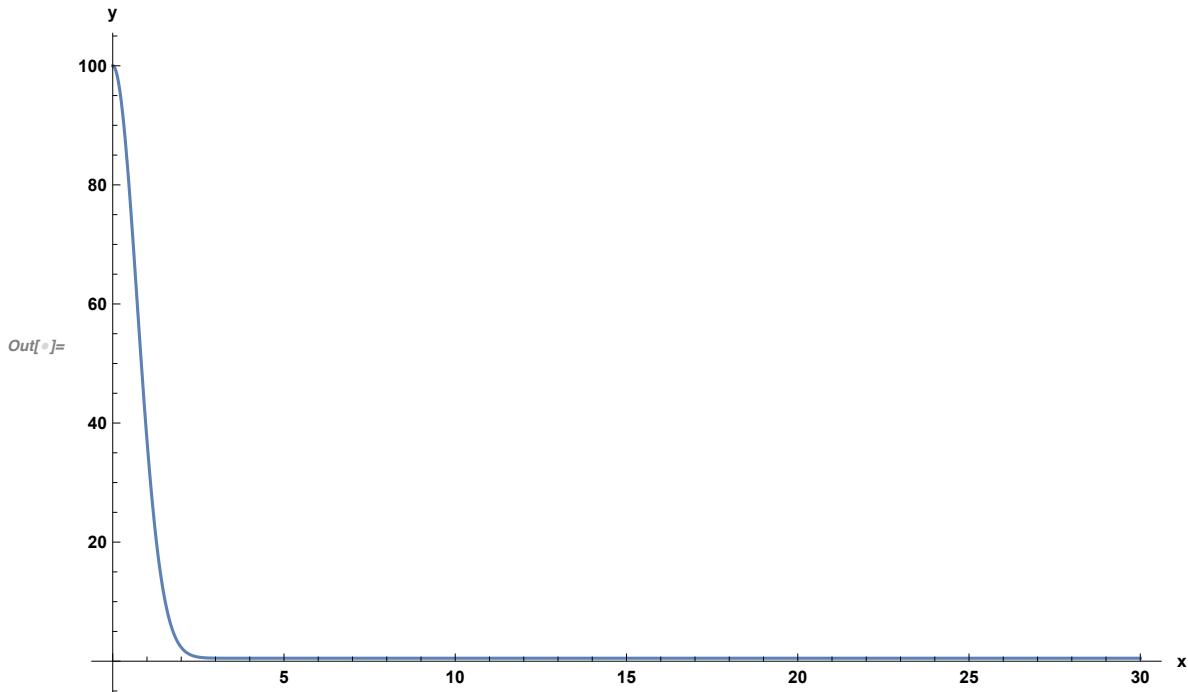

---

## Solve First-Order ODEs

```
In[7]:= s = NDSolve[{y'[x] == x - 2 x y[x], y[0] == 100}, y, {x, 0, 30}]
```

```
Out[7]= {y → InterpolatingFunction[ +  Domain: {{0., 30.}} Output: scalar ] } }
```

```
In[8]:= Plot[Evaluate[y[x] /. s], {x, 0, 30}, PlotRange -> All, AxesLabel -> {"x", "y"}]
```



## Solve the general solution of Second-Order ODEs

```
In[9]:= s = DSolve[{y''[x] + 2 y[x] + 1 == -2 x}, y, {x, 0, 30}]
```

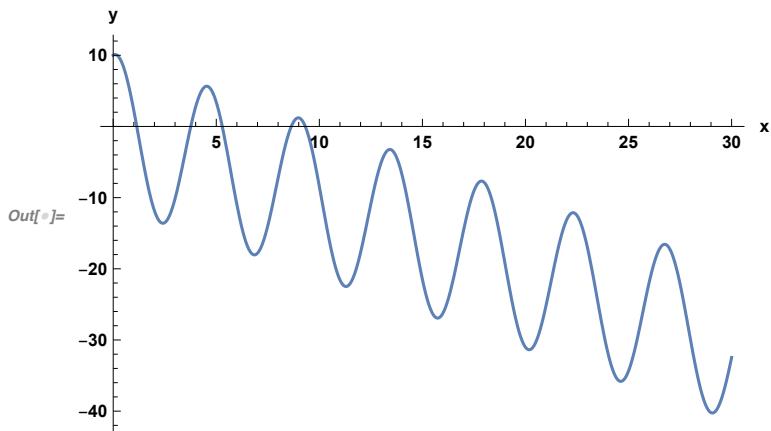
```
Out[9]= {y -> Function[{x}, -1/2 - x + C[1] Cos[Sqrt[2] x] + C[2] Sin[Sqrt[2] x]]}}
```

## Solve the IVP of Second-Order ODEs

```
In[10]:= s = DSolve[{y''[x] + 2 y[x] + 1 == -2 x, {y[0] == 10, y'[0] == 2}}, y, {x, 0, 30}]
```

```
Out[10]= {y -> Function[{x}, 1/2 (-1 - 2 x + 21 Cos[Sqrt[2] x] + 3 Sqrt[2] Sin[Sqrt[2] x])]}
```

```
In[4]:= Plot[Evaluate[y[x] /. s], {x, 0, 30}, PlotRange -> All, AxesLabel -> {"x", "y"}]
```



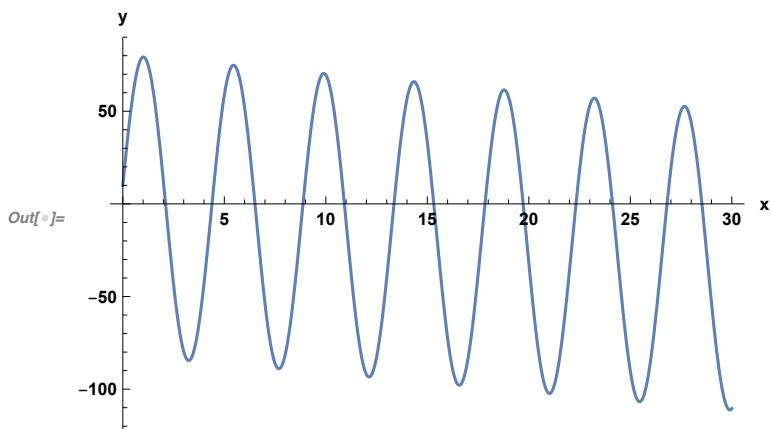
## Solve the BVP of Second-Order ODEs

```
In[5]:= s = DSolve[{y''[x] + 2 y[x] + 1 == -2 x, {y[0] == 10, y'[1] == 2}}, y, {x, 0, 30}]
```

Out[5]=

$$\left\{ \left\{ y \rightarrow \text{Function}[\{x\}, \frac{1}{2} (-1 - 2x + 21 \cos[\sqrt{2}x] + 3 \sec[\sqrt{2}] (\sqrt{2} + 7 \sin[\sqrt{2}]) \sin[\sqrt{2}x])] \right\} \right\}$$

```
In[6]:= Plot[Evaluate[y[x] /. s], {x, 0, 30}, PlotRange -> All, AxesLabel -> {"x", "y"}]
```

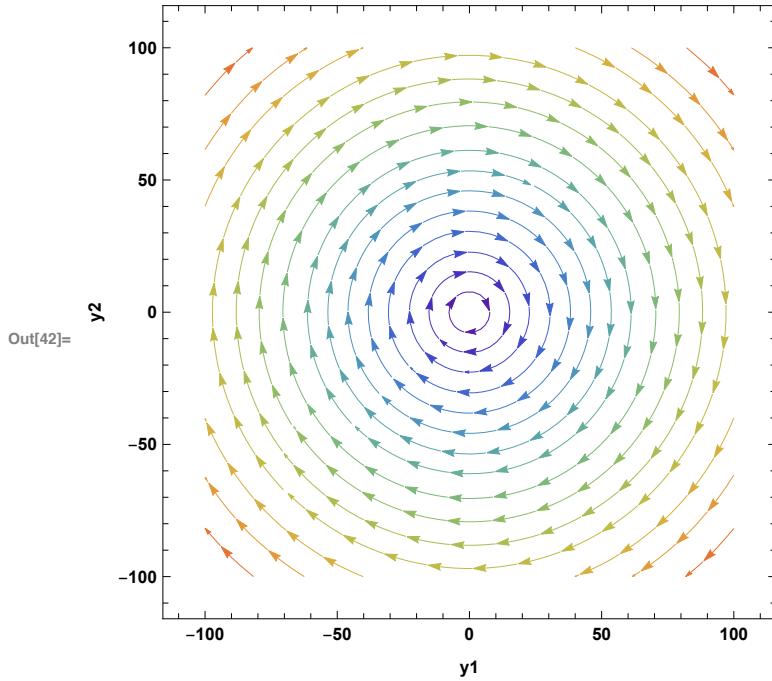


## Plot the phase portrait a system of 1st-Order ODEs

```
In[40]:= (*example 1*)
```

```
In[41]:= w1 = w2 = 10;
```

```
In[42]:= StreamPlot[{w1 * y2, -w2 * y1}, {y1, -100, 100}, {y2, -100, 100},
StreamColorFunction -> "Rainbow", FrameLabel -> {"y1", "y2"}]
```



```
In[43]:= (*example 2*)
```

```
In[44]:= w1 = 15; w2 = 5;
```

```
In[45]:= StreamPlot[{w1 * y2, -w2 * y1}, {y1, -100, 100}, {y2, -100, 100},
StreamColorFunction -> "Rainbow", FrameLabel -> {"y1", "y2"}]
```

